

Table of Contents

6 th Grade Year-at-a-Glance	
Unit #1: Number Sense with Fractions, Decimals, and Whole Numbers	
Unit #2: Ratio and Unit Rates	
Unit #3: Algebraic Expressions	
Unit #4: Equations and Inequalities	
Unit #5: Rational Numbers	
Unit #6: Geometry	
Unit #7: Statistics and Probability	

	6 th Grade Year-at-a-Glance						
	Month	Unit	Content Standards				
District Benchmark 1	September/October	Unit #1	6.NS.1 6.NS.2				
*Alignment TBD		Number Sense with Fractions, Decimals, and Whole Numbers	6.NS.3 6.NS.4				
	November	Unit #2 Ratios and Unit Rates	6.RP.1 6.RP.2 6.RP.3				
District Benchmark 2 *Alignment TBD	December/January	Unit #3 Algebraic Expressions	6.EE.1 6.EE.2 6.EE.3 6.EE.4				
			6.EE.5 6.EE.6				
District Benchmark 3	February/March	Unit #4 Equations and Inequalities	6.EE.7 6.EE.8 6.EE.9 6.NS.3				
*Alignment TBD	March/April	Unit #5 Rational Numbers	6.NS.5 6.NS.6 6.NS.7 6.NS.8				
CAASPP (Smarter Balanced Summative Test)	April/May	Unit #6 Geometry	6.G.1 6.G.2 6.G.3 6.G.4 6.NS.8				
	May/June	Unit #7 Statistics and Probability	6.SP.1 6.SP.2 6.SP.3 6.SP.4 6.SP.5				

Unit #1: Number Sense with Fractions, Decimals, and Whole Numbers

(Approx. # of Days 35-40)

Content Standards: 6.NS.1-4

In this unit, students will work with multiplication and division of fractions, decimals, and whole numbers.

Common Core State Standards–Mathematics:

The Number System 6.NS

Apply and extend previous understandings of multiplication and division to divide fractions by fractions.

Interpret and compute quotients of fractions, and solve word problems involving division of fractions by fractions, e.g., by using visual fraction models and equations to represent the problem. For example, create a story context for (2/3) ÷ (3/4) and use a visual fraction model to show the quotient; use the relationship between multiplication and division to explain that (2/3) ÷ (3/4) = 8/9 because 3/4 of 8/9 is 2/3. (In general, (a/b) ÷ (c/d) = ad/bc) How much chocolate will each person get if 3 people share 1/2 lb. of chocolate equally? How many 3/4-cup servings are in 2/3 of a cup of yogurt? How wide is a rectangular strip of land with length 3/4 mi and area 1/2 square mi?

Compute fluently with multi-digit numbers and find common factors and multiples.

- 2. Fluently divide multi-digit numbers using the standard algorithm.
- 3. Fluently add, subtract, multiply, and divide multi-digit decimals using the standard algorithm for each operation.
- 4. Find the greatest common factor of two whole numbers less than or equal to 100 and the least common multiple of two whole numbers less than or equal to 12. Use the distributive property to express a sum of two whole numbers 1–100 with a common factor as a multiple of a sum of two whole numbers with no common factor. For example, express 36 + 8 as 4 (9 + 2).

Standards for Mathematical Practice:

SMP.4 – Model with mathematics SMP.6 – Attend to precision

SEL Competencies:

Self-awareness Self-management Social awareness Relationship skills Responsible decision making

ELD Standards to Support Unit

Part I: Interacting in Meaningful Ways:

- A. Collaborative:
 - 2. Interacting with others in written English in various communicative forms
 - 4. Adapting language choices to various contexts
- B. Interpretive:
 - 5. Listening actively to spoken English in a range of social and academic contexts.
- C. Productive:
 - 11. Supporting own opinions and evaluating others' opinions in speaking and writing.

Part II: Learning About How English Works

• Expanding and Enriching Ideas

5. Modifying to add details.

- Connecting and Condensing Ideas
 - 6. Connecting Ideas
 - 7. Condensing Ideas

	Unit #1 Number Sense with Fractions, Decimals, and Whole Numbers						
Essential Questions	Assessments for Learning	Sequence for Learning Outcomes 6.NS.14	Strategies for Teaching and Learning	Differentiation e.g. EL, SpEd, GATE	Resources		
Essential Questions are thought- provoking, open-ended questions to be used within daily lessons that and are therefore connected to the Sequence of Learning Outcomes	Learning address Diagnostic, Formative, and Summative assessments used throughout the unit to inform instruction connected to the Sequence of Learning Outcomes. <i>Note: These</i> <i>assessments are</i> <i>suggested, not</i> <i>required.</i>	Sequence of Learning Outcomes is intentionally organized for student success. Each outcome is not necessarily intended to be taught within one class session. Each Outcome begins with Students will be able to	 Strategies to support Unit: From the CA Mathematics Framework <u>"Instructional Strategies"</u> chapter provides research-based strategies for teaching math, K-12 <u>"Supporting High Quality Common Core</u> <u>Instruction"</u> chapter addresses the development, implementation, and maintenance of high-quality, standards-based mathematics instructional programs <u>"Universal Design for Learning"</u> from CAST, the Center for Applied Special Technology 	Differentiation support for Unit: Use of math journals for differentiation and formative assessment. See <u>Teaching Channel</u> Video Flexible grouping: • Content • Interest • Project/product • Level (Heterogeneous/ Homogeneous) Tiered: 1. Independent Management Plan (Must Do/May Do) 2. Grouping • Content • Rigor w/in the concept	 strategies, additional resources/tools and misconceptions by standard. P. 14-22 The Number System 		
 How can you use prime factorization to find the greatest common factor (GCF) and least 	For learning outcomes 1-4: From Mathematics Assessment	 Factor composite numbers up to 100 and use the prime factors to list all factor pairs. 6.NS.4 	From SCUSD resource development: <u>Strategy for finding factor pairs through prime</u> <u>factorization</u>	 Project-based learning Homework Grouping Formative 	CA Framework p. 25-31 Flipbook p. 21-23 NC Unpacking p. 20-22 enVision, Topic 6		

	Unit #1 Number Sense with Fractions, Decimals, and Whole Numbers							
Essential Questions	Assessments for Learning	Sequence for Learning Outcomes 6.NS.14	Strategies for Teaching and Learning	Differentiation e.g. EL, SpEd, GATE	Resources			
common multiple (LCM) of two numbers at the same time?	Resource Service (MARS) <u>"Factors</u> <u>and Multiples"</u> From Illustrative Mathematics:	2) Use prime factorization to greate		Assessment Anchor Activities: • Content-related • Tasks for early	Lesson 6-1 "Greatest Common Factor"			
 How can you use prime factorization to find the greatest common factor (GCF) and least common multiple (LCM) of two numbers at the same time? 		 2) Use prime factorization to create lists of factor pairs to find the greatest common factor of two numbers (1–100). 6.NS.4 	From SCUSD resource development: <u>Strategy for using primes to find GCF</u> As an extension to Learning Outcome 2, students should make the connection to the fact that the GCF of two numbers is the product of all common prime factors. Study of GCF and LCM may provide opportunity for review of fraction operations learned in	finishers Game Investigation Partner Activity Stations Depth and Complexity Prompts/Icons: Depth	CA Framework p. 25-31 Flipbook p. 21-23 NC Unpacking p. 20-22 enVision, Topic 6 • Lesson 6-1 "Greatest Common Factor"			
 How does finding all the prime factors of two numbers help to find all common factors including the GCF? 		 3) Use greatest common factor to solve real world problems. See example * 6.NS.4 	number of cupcakes in each box. What is the greatest number of cupcakes that can fit in a box? How many boxes will they have altogether? Solution: 2 boxes of 16 and 3 boxes of 16 for a	 Language of the Discipline Patterns Unanswered Questions Rules Trends Big Ideas Complexity 	CA Framework p. 25-31 Flipbook p. 21-23 NC Unpacking p. 20-22 enVision, Topic 6 • Lesson 6-1 "Greatest Common Factor" Common Core Sheets on GCF			
 How does finding the GCF of two numbers lead you to find the 'LC"M of two numbers? 		 4) Find the least common multiple of two numbers (1-12) by creating organized lists of multiples of each number. 6.NS.4 	total of 5 boxes of 16 cupcakes.	Differentiation Resources from <u>SCUSD Wikispace:</u>	 <u>CA Framework</u> p. 25-31 See "The Ladder Method for Finding GCF and LCM" p. 31 <u>Flipbook</u> p. 21-23 <u>NC Unpacking</u> p. 20-22 <i>enVision</i>, Topic 6 			

	Unit #1 Number Sense with Fractions, Decimals, and Whole Numbers					
Essential Questions	Assessments for Learning	Sequence for Learning Outcomes 6.NS.14	Strategies for Teaching and Learning	Differentiation e.g. EL, SpEd, GATE	Resources	
					Lesson 6-2 "Least Common Multiple" <u>Common Core Sheets on LCM</u>	
For Learning Outcomes	For Learning	5) Analyze a decimal number,	From SCUSD resource development:		CA Framework p. 25-31	
5 — 9:	Outcome 5:	representing it numerically and	Strategy for Writing Decimals as Fractions in		Flipbook p. 20	
		pictorially, as both a single	Multiple Ways		NC Unpacking p. 18-19	
What are the	From Inside	fraction and as a sum of the place				
multiple ways to	Mathematics:	value pieces of the fraction	Both Outcomes 5 and 9 can be tied into		Worksheets to help with guided practice:	
decompose 3.125 as		(e.g. 6.32 =	outcomes 6-8 when used a guided warm up,		Math Goodies	
a fraction?	<u>"Sewing"</u>		review of prior knowledge, or an independent		Mathworksheetsland.com	
		$6 + \frac{32}{100} = 6 + \frac{30}{100} + \frac{2}{100} =$	challenge problem.		EngageNY Use topics 6-15 for 6.NS.3	
 How do you know what the denominator is 		$6 + \frac{3}{10} + \frac{2}{100}$				
when writing a		in order to recognize that ten or				
decimal number as		more of any place value can be				
a fraction?		re-written in a place value				
		representing the next smaller				
		power of ten.				
		6.NS.3				

	Unit #1 Number Sense with Fractions, Decimals, and Whole Numbers						
Essential Questions	Assessments for Learning	Sequence for Learning Outcomes 6.NS.14	Strategies for Teaching and Learning	Differentiation e.g. EL, SpEd, GATE	Resources		
 When adding, why does "twelve-hundredths" get re-grouped as "one-tenth" and "two-hundredths"? What similarities are there between whole digit addition/subtracttion and decimal addition/subtracttion? Why and when do we use common denominators with addition, subtraction, and division? 	For Learning Outcomes 6 – 9: From Illustrative Mathematics: <u>"Jayden's Snacks"</u>	 6) Add and subtract multi-digit decimals with the same terminating place value (without re-grouping (e.g. 6.32 + 3.15), or borrowing, by decomposing the quantities into terms of whole numbers and fractions to understand place value. See link to strategy for teaching this learning experience. 6.NS.3 7) Add and subtract multi-digit decimals with different terminating place value (e.g. 6.3 + 3.561), without re-grouping, by decomposing the quantities into terms of whole numbers and fractions to understand place value (e.g. 6.3 + 3.561), without re-grouping, by decomposing the quantities into terms of whole numbers and fractions to understand place value. 6.NS.3 8) Add and subtract multi-digit decimals with re-grouping (e.g. 6.79 + 3.54 or 6.3 - 4.83), by decomposing the quantities into terms of whole numbers and fractions to understand place value. See link to strategy for teaching this learning experience. 	 From SCUSD resource development: <u>Strategies for Using Place Value to Add and</u> <u>Subtract Decimals</u> p. 2 When performing all operations with decimals and fractions, incorporate estimation into the experience throughout the problem. From SCUSD resource development: <u>Strategies for Using Place Value to Add and</u> <u>Subtract Decimals</u> p. 3 When performing all operations with decimals and fractions, incorporate estimation into the experience throughout the problem. 		 CA Frameworkp. 25-31 Flipbook p. 20 NC Unpacking p. 18-19 enVision, Topic 4 Lesson 4-1, "Estimating Sums and Differences Lesson 4-2, "Evaluating Addition and Subtraction Expressions" Lesson 4-3, "Solving Addition and Subtraction Equations" CA Framework p. 25-31 Flipbook p. 20 NC Unpacking p. 18-19 enVision, Topic 4 Lesson 4-1, "Estimating Sums and Differences Lesson 4-2, "Evaluating Addition and Subtraction Expressions" Lesson 4-3, "Solving Addition and Subtraction Expressions" Lesson 4-3, "Solving Addition and Subtraction Equations" CA Framework p. 25-31 Flipbook p. 20 NC Unpacking p. 18-19 enVision, Topic 4 Lesson 4-1, "Estimating Sums and Differences Lesson 4-2, "Evaluating Addition and Subtraction Equations" CA Framework p. 25-31 Flipbook p. 20 NC Unpacking p. 18-19 enVision, Topic 4 Lesson 4-1, "Estimating Sums and Differences Lesson 4-2, "Evaluating Addition and Subtraction Expressions" Lesson 4-3, "Solving Addition and Subtraction Expressions" Lesson 4-3, "Solving Addition and Subtraction Expressions" 		

		Unit #1 Number	Sense with Fractions, Decimals, and Whole N	umbers	
Essential Questions	Assessments for Learning	Sequence for Learning Outcomes 6.NS.14	Strategies for Teaching and Learning	Differentiation e.g. EL, SpEd, GATE	Resources
		 9) Make connections to strategies for addition and subtraction with multi-digit whole numbers. 6.NS.3 	 Strategies to connect include decomposition, adding up, and finally, standard algorithms. From SCUSD resource development/Wikispace: Strategy for <u>"Changing Decimal and Fraction Addition and Subtraction into Multi-Digit Whole Number Addition and Subtraction"</u> Decompose numbers into expanded form From SCUSD resource development/Wikispace: Strategy for <u>Adding Up</u> 		 <u>CA Framework</u> p. 25-31 <u>Flipbook</u> p. 20 <u>NC Unpacking</u> p. 18-19 <i>enVision</i>, Topic 4 Lesson 4-1,"Estimating Sums and Differences Lesson 4-2, "Evaluating Addition and Subtraction Expressions" Lesson 4-3, "Solving Addition and Subtraction Equations"
 What would be a reasonable estimate for the product of 3.8 and 5.12? (extend this question to addition, subtraction, and division of decimals) 	For Learning Outcomes 10-11: From Illustrative Mathematics: " <u>Reasoning about</u> <u>Multiplication and Division and Place</u> <u>Value, Part 1"</u>	 10) Estimate products of decimal numbers using front-end estimation and by rounding to the largest place value. Compare the results the estimations without finding the exact answer. 6.NS.3 	 From SCUSD resource development/Wikispace: Strategy for <u>"Multiplying Decimals"</u> Use rounding as a tool to estimate reasonableness of decimal placement throughout multiplication of decimals When performing all operations with decimals and fractions, incorporate estimation into the experience throughout the problem. 		 <u>CA Framework</u> p. 25-31 <u>Flipbook</u> p. 20 <u>NC Unpacking</u> p. 18-19 <i>enVision</i>, Topic 4 Lesson 4-4 "Estimating Products"
 How do you know what the denominator is when writing a decimal number as a fraction? For multiplication, 		11) Write decimals as fractions and multiply, using the denominator of the product to determine place value.6.NS.3	 From SCUSD resource development/Wikispace: Strategy for <u>"Multiplying Decimals"</u> When performing all operations with decimals and fractions, incorporate estimation into the experience throughout the problem. 		 <u>CA Framework</u> p. 25-31 <u>Flipbook</u> p. 20 <u>NC Unpacking</u> p. 18-19 <i>enVision</i>, Topic 4 Lesson 4-5 "Multiplying Decimals"

	Unit #1 Number Sense with Fractions, Decimals, and Whole Numbers					
Essential Questions	Assessments for Learning	Sequence for Learning Outcomes 6.NS.14	Strategies for Teaching and Learning	Differentiation e.g. EL, SpEd, GATE	Resources	
why is finding a common denominator not helpful?						
For Learning Outcomes 12-14:	For Learning Outcomes 12-18:	12) Divide multi-digit whole numbers using scaffold long division.	Recognize the connection between division and repeated subtraction.		CA Framework p. 25-31 Flipbook p. 18-19 NC Unpacking p. 16-17	
 Which method for dividing multi-digit whole numbers do you prefer – "scaffolded" or "stacking" – and 	• <u>"Baking Cookies"</u>	6.NS.2	Write quotients as mixed numbers where appropriate.		Example of Scaffold Division from SCUSD resource development Long Division Scaffolding video from showme.com	
"stacking" –and why?	 <u>"Price per Pound</u> and Pound per <u>Dollar"</u> <u>"Reasoning about</u> <u>Multiplication and</u> <u>Division and Place</u> <u>Value"</u> 	 13) Divide multi-digit whole numbers using stacked long division recognizing place value throughout the process. 6.NS.2 	Stacked division is a method of using repeated subtraction for division which connects place value to the standard division algorithm. Write quotients as mixed numbers where appropriate.		 <u>CA Framework</u> p. 25-31 "Connecting Place Value and Division Algorithms", p. 27 <u>Flipbook</u> p. 18-19 <u>NC Unpacking</u> p. 16-17 <u>Partial Quotients (Stacked) for Division</u> video from YouTube 	

		Unit #1 Number	Sense with Fractions, Decimals, and Whole N	lumbers	
Essential Questions	Assessments for Learning	Sequence for Learning Outcomes 6.NS.14	Strategies for Teaching and Learning	Differentiation e.g. EL, SpEd, GATE	Resources
	• <u>"The Florist Shop"</u>	14) Make connections between different strategies for long division of multi-digit whole numbers building towards fluency.	Strategies to connect include scaffold division, stacked division, and standard division algorithms. Write quotients as mixed numbers where		 <u>CA Framework</u> p. 25-31 Scaffold Division example, p. 26 <u>Flipbook</u> p. 18-19 <u>NC Unpacking</u> p. 16-17
		6.NS.2	appropriate.		 enVision, Topic 5: Lesson 5-1 "Estimating Quotients: 2-Digit Divisors" Lesson 5-2 "Dividing Whole Numbers: 2-Digit Divisors" Lesson 5-3 "More Dividing Whole Numbers"
 Why is finding a common denominator helpful for dividing fractions by fractions? How do you know what the denominator is when writing a decimal number as 	 For Learning Outcomes 12-18: From Illustrative Mathematics: <u>"Baking Cookies"</u> <u>"Price per Pound</u> and Pound per Dollar" 	15) Divide fractions with common denominators with models.6.NS.1	From SCUSD resource development: Strategies for Dividing Fractions		 <u>CA Framework</u> p. 20-25 <u>Flipbook</u> p. 15-17 <u>NC Unpacking</u> p. 14-15 <i>enVision</i>, Topic 6 Lesson 6-3 "Understanding Division of Fractions", p.156A -157B Lesson 6-4 "Dividing Whole Numbers by Fractions" "Math Background," p.158A "Problem-Based Interactive
 a fraction? Why is finding a common denominator 	 <u>"Reasoning about</u> <u>Multiplication and</u> <u>Division and Place</u> <u>Value"</u> "The Florist Shop" 	 16) Divide fractions without common denominators with models to find common denominator and 	•		Learning,"p.158B Lesson 6-5 "Modeling Division of Fractions", p.160A-161B <u>CA Framework</u> p. 20-25 <u>Flipbook</u> p. 15-17 NC Unpacking p. 14-15

	Unit #1 Number Sense with Fractions, Decimals, and Whole Numbers						
Essential Questions	Assessments for Learning	Sequence for Learning Outcomes 6.NS.14	Strategies for Teaching and Learning	Differentiation e.g. EL, SpEd, GATE	Resources		
 helpful for dividing fractions by fractions? Why and when do we use common denominators with addition, subtraction, and division? 		to show that division means how many of one quantity goes into another. 6.NS.1			 enVision, Topic 6 Lesson 6-8 "Dividing Mixed Numbers" "Problem-Based Interactive Learning," p.166B 		
 Why and when do we use common denominators with addition, subtraction, and division? 	For Learning Outcomes 12-18: From Illustrative Mathematics:	 17) Divide fractions by fractions "straight across" where the numerators are divisible and the denominators are divisible. (Example) Include the special case of common denominators. 6.NS.1 	From SCUSD resource development: Strategies for Dividing Fractions		 <u>CA Framework</u> p. 20-25 <u>Flipbook</u> p. 15-17 <u>NC Unpacking</u> p. 14-15 <i>enVision, Topic 6</i> Lesson 6-5, "Modeling Division of Fractions" I would have the students find an equivalent fraction with common denominators before solving problems 		
 Why is finding a common denominator helpful for dividing fractions by fractions? Why and when do 	 <u>"Baking Cookies"</u> <u>"Price per Pound</u> and Pound per Dollar" "Reasoning about 	 18) Divide fractions by fractions "straight across" where only one pair, numerator or denominator, are originally divisible by finding a fraction equivalent to the dividend. 	From SCUSD resource development: Strategies for Dividing Fractions		CA Framework p. 20-25 <u>Flipbook</u> p. 15-17 <u>NC Unpacking</u> p. 14-15 <i>enVision, Topic 6</i> • Lesson 6-5, "Modeling Division of Fractions" ○ I would have the students find an		
 Why and when do we use common denominators with addition, subtraction, and division? 	 <u>Multiplication and</u> <u>Division and Place</u> <u>Value</u>" <u>"The Florist Shop"</u> 	6.NS.1			equivalent fraction with common denominators before solving problems		

			Unit #1 Number	Sense with Fractions, Decimals, and Whole N	lumbers	
E	Essential Questions	Assessments for Learning	Sequence for Learning Outcomes 6.NS.14	Strategies for Teaching and Learning	Differentiation e.g. EL, SpEd, GATE	Resources
•	Why and when do we use common denominators with addition, subtraction, and division?	For Learning Outcomes 19-21: From Illustrative Mathematics:	19) Divide fractions by fractions "straight across" where no pairs are originally divisible by finding a common denominator. 6.NS.1	From SCUSD resource development: Strategies for Dividing Fractions		CA Framework p. 20-25 Flipbook p. 15-17 NC Unpacking p. 14-15 enVision- Topic 6 • Lesson 6-6, "Dividing Fractions"
•	Why can you multiply by the reciprocal when dividing fractions?	<u>"Movie Tickets"</u> "Setting Goals"				• Problems 11, 12,15, 19- 21, 28
•	Why can you multiply by the reciprocal when dividing fractions?		20) Analyze different cases of dividing fractions by fractions to generalize that one can multiply by the reciprocal.6.NS.1	 "Teaching the invert and multiply model for dividing fractions without developing an understanding of why it works can confuse students and interfere with their ability to apply division of fractions to solve word problems." (CA Math Framework p.24) From SCUSD resource development: <u>Strategies for Dividing Fractions</u> 		 <u>CA Framework</u> p. 20-25 <u>Flipbook</u> p. 15-17 <u>NC Unpacking</u> p. 14-15 <i>enVision</i>, Topic 6 Lesson 6-6 "Dividing Fractions"
•	How are dividing with whole numbers and dividing with decimals similar and different?		21) Divide multi-digit decimals with different terminating place values by writing as two fractions, finding a common denominator, then dividing straight across in order to perform long division	From SCUSD resource development: <u>Example of dividing multi-digit decimals with</u> <u>whole number quotients</u> *For Learning Outcomes 21-22, all quotients in decimal division problems should be whole		CA Framework p. 25-31 Flipbook p. 20 NC Unpacking p. 18-19 enVision, Topic 5 • Lesson 5-5 "Dividing Decimals" p. 134
•	How can dividing with decimals be made easier by converting to fractions?		with whole numbers*. 6.NS.3	numbers. Learning Outcomes 24-26 will concentrate on decimal quotients that terminate.		(problem 23)

		Unit #1 Number	Sense with Fractions, Decimals, and Whole N	umbers	
Essential Questions	Assessments for Learning	Sequence for Learning Outcomes 6.NS.14	Strategies for Teaching and Learning	Differentiation e.g. EL, SpEd, GATE	Resources
 How would you explain the reason we can "move the decimal" to create whole numbers and perform long division? 	For Learning Outcomes 22-23: From Illustrative Mathematics: <u>"Reasoning around</u> <u>Multiplication and</u>	 22) Analyze the process used for dividing decimals to generalize and create short-cuts of moving the decimal and dividing whole numbers*. 6.NS.3 			 <u>CA Framework</u> p. 25-31 <u>Flipbook</u> p. 20 <u>NC Unpacking</u> p. 18-19 <i>enVision Topic 5</i> Lesson 5-5, "Dividing Decimals"
 What is really happening when we "bring up the decimal" when doing the traditional division algorithm? 	Division and Place Value Part I" "Reasoning around Multiplication and Division and Place Value Part II"	 23) Understand that when dividing a decimal by a whole number, the integrity of the place value is maintained by first multiplying by the appropriate power of 10, completing the division, and then dividing by the same power of 10 in order to maintain identity. 6.NS.3 	Learning Outcome 23 provides the justification for why we can "bring up the decimal" when using the traditional division algorithm. See <u>"Dividing a Decimal by a Whole Number"</u> . Ex: $2.4 \div 6 = \frac{2.4}{6} \times \frac{10}{1} \times \frac{1}{10} = \frac{24}{6} \times \frac{1}{10} = 4 \times \frac{1}{10} = \frac{4}{10}$		 <u>CA Framework</u> p. 25-31 <u>Flipbook</u> p. 20 <u>NC Unpacking</u> p. 18-19 <i>enVision Topic 5</i> Lesson 5-5, "Dividing Decimals"
 How do we temporarily remove the decimal point when doing division? How do we re-establish the decimal point (place value)? 	For Learning Outcome 24: From Illustrative Mathematics: <u>"Grandma's Gifts"</u> From SERP – Strategic Education Research Partnership:	 24) Divide a decimal number by a whole number where the quotient is a decimal (e.g. 56.58 ÷ 3 = 18.86) using the algorithms developed in unit 1, paying close attention to place value. 6.NS.3 	<i>For Learning Outcomes 24 and 25,</i> there should be no need to extend place value by adding zeroes. (This takes place in Learning Outcome 26.) All decimals should be terminating.		 <u>CA Framework p. 25-31</u> <u>Flipbook p. 20</u> <u>NC Unpacking p. 18-19</u> <u>Student work examples</u> of Learning Outcomes 24-27 <i>enVision, Topic 5</i> Lesson 5-4, "Dividing Decimals by a Who Number"

		Unit #1 Number	Sense with Fractions, Decimals, and Whole N	umbers	
Essential Questions	Assessments for Learning	Sequence for Learning Outcomes 6.NS.14	Strategies for Teaching and Learning	Differentiation e.g. EL, SpEd, GATE	Resources
Why do we "move the decimal" (Get rid of the decimal) in the divisor when we divide decimals?	<u>"No Matter How</u> <u>You Slice It"</u> For Learning Outcome 25: From Illustrative Mathematics <u>"Buying Gas"</u>	 25) Divide a decimal number by a decimal number where the quotient is a decimal (e.g. 16.728 ÷ 3.4 = 4.92) using the algorithms developed in Unit 1, multiplying by powers of 10 to make the divisor a whole number. 6.NS.3 			CA Framework p. 25-31 Flipbook p. 20 NC Unpacking p. 18-19 enVision, Topic 5 • Lesson 5-5 "Dividing Decimals"
 Why are we allowed to add zeroes to the end of a number to the right of the decimal? Why can't we do this to the left of the decimal? 	For Learning Outcome 26: From EngageNY: <u>"Dividing Decimals"</u> (With adding zeroes)	 26) Divide a decimal number by a decimal number where the quotient is a decimal (e.g. 3.3 ÷ 1.2 = 2.75) using the algorithms developed in unit 1, extending the place value of the dividend by adding zeroes. 6.NS.3 	When doing Learning Outcome 26, verify that extending the place value by adding zeroes does not change the value of the dividend		 <u>CA Framework p. 25-31</u> <u>Flipbook p. 20</u> <u>NC Unpacking p. 18-19</u> enVision, Topic 5 Lesson 5-4 "Dividing Decimals by a Whole Number" Another Example – Step 3 p.132

Unit #2: Ratio and Unit Rates	
(Approx. # of Days 20)	
Content Standards: 6.RP.1, 2, 3	
In this unit, students will be able to make and use ratios and proportions appropriately.	
Common Core State Standards-Mathematics:	
Ratio and Proportional Relationships 6.RP	
Understand ratio concepts and use ratio reasoning to solve problems	
 Understand the concept of a ratio and use ratio language to describe a ratio relationship between two quantities. For example, "The ratio of wings to beaks in the bird house at the zoo was 2:1, because every 2 wings there was 1 beak." "For every vote candidate A received, candidate C received nearly three votes." 	for
 Understand the concept of a unit rate a/b associated with a ratio a:b with b ≠ 0, and use rate language in the context of a ratio relationship. For example, "This recipe has a ratio of 3 cups of flour to 4 custors sugar, so there is 3/4 cup of flour for each cup of sugar." "We paid \$75 for 15 hamburgers, which is a rate of \$5 per hamburger." 	ıps of
3. Use ratio and rate reasoning to solve real-world and mathematical problems, e.g., by reasoning about tables of equivalent ratios, tape diagrams, double number line diagrams, or equations.	
a. Make tables of equivalent ratios relating quantities with whole number measurements, find missing values in the tables, and plot the pairs of values on the coordinate plane. Use tables to compare ra	tios.
b. Solve unit rate problems including those involving unit pricing and constant speed. For example, if it took 7 hours to mow 4 lawns, then at that rate, how many lawns could be mowed in 35 hours? At w rate were lawns being mowed?	vhat
c. Find a percent of a quantity as a rate per 100 (e.g., 30% of a quantity means 30/100 times the quantity); solve problems involving finding the whole, given a part and the percent.	
d. Use ratio reasoning to convert measurement units; manipulate and transform units appropriately when multiplying or dividing quantities.	
standards for Mathematical Practice of Emphasis:	
MP.2 – Reason abstractly and quantitatively	
MP.4 – Model with mathematics	
MP.6 – Attend to precision.	
MP.7 - Look for and make use of structure.	

ELD Standards to Support Unit:

Part I: Interacting in Meaningful Ways:

- D. Collaborative:
 - 3. Interacting with others in written English in various communicative forms
 - 6. Adapting language choices to various contexts
- E. Interpretive:
 - 7. Listening actively to spoken English in a range of social and academic contexts.
- F. Productive:
 - 11. Supporting own opinions and evaluating others' opinions in speaking and writing.

Part II: Learning About How English Works

- Expanding and Enriching Ideas
 - 5. Modifying to add details.
- Connecting and Condensing Ideas
 - 6. Connecting Ideas
 - 7. Condensing Ideas

- SEL Competencies:
- Self-awareness
- Self-management
- Social awareness
- Relationship skills
- Responsible decision making

		Unit #2 Ratio and L	Jnit Rates		
Essential Questions	Assessments for Learning	Sequence of Learning Outcomes 6.RP.1, 6.RP.2, 6.RP.3	Strategies for Teaching and Learning	Differentiation (EL/SpEd/GATE)	Resources
Essential Questions are thought- provoking, open-ended questions to be used within daily lessons that and are therefore connected to the Sequence of Learning Outcomes	Assessments for Learning address Diagnostic, Formative, and Summative assessments used throughout the unit to inform instruction connected to the Sequence of Learning Outcomes. <i>Note: These assessments are suggested, not required.</i>	Sequence of Learning Outcomes is intentionally organized for student success. Each outcome is not necessarily intended to be taught within one class session. Each Outcome begins with Students will be able to	Strategies to support Unit: From the CA Mathematics Framework • <u>"Instructional</u> Strategies" chapter provides research-based strategies for teaching math, K-12 • <u>"Supporting High</u> Quality Common Core Instruction" chapter addresses the development, implementation, and maintenance of high-quality, standards-based mathematics instructional programs <u>"Universal Design for</u> Learning" from CAST, the Center for Applied	Differentiation support for Unit: Use of math journals for differentiation and formative assessment. See <u>Teaching</u> <u>Channel Video</u> Flexible grouping: Content Interest Project/produ ct Level (Heterogeneo us/ Homogeneous) Tiered: 3. Independent Management Plan (Must Do/May Do) 4. Grouping	 progression of a topic across a number of grade levels, informed both by research on children's cognitive development and by the logical structure of mathematics. <u>Progressions on Ratios and</u> <u>Proportional Relationships</u> Overview p. 2-4 Grade 6 p. 5-7 <u>Kansas Association of Teachers of</u> <u>Mathematics (KATM) 6th Grade Flipbook</u>

				Unit #2 Ratio and U	nit Rates			
	Essential Questions	Assessments for Learning		Sequence of Learning Outcomes 6.RP.1, 6.RP.2, 6.RP.3	Strategies for Teaching and Learning		erentiation SpEd/GATE)	Resources
					Special Technology	0	Content Rigor w/in the concept	instructional strategies, additional resources/tools and misconceptions by standard. P. 29-35 <i>Expressions and Equations</i>
•	What kind of problems can I solve with ratios? When is it useful to be able to relate one quantity		1)	Use ratio and rate language, orally and in writing to describe the relationship between two quantities including for each, per, to, each, 1/5,	Omit discussion of percent in ratio and rate language until experience 8	0	sed learning	<u>CA Framework</u> p. 7-9 <u>Flipbook</u> p. 7-9 <u>NC Unpacking</u> p. 7
•	to another? How can I compare two different quantities? How are ratios and rates	<u>Games at Recess</u> The Escalator		1:5, etc. 6.RP.1	For outcome 2, all problems are "simple"	0	1 0	 enVision, Topic 9: Lesson 9-1- "Understanding Ratios enVision, Topic 10: Lesson 10-8 – "Writing to Explain"
•	similar and different? Why is unit rate	For Learning Outcomes 2-5: From Illustrative Mathematics:	2)	Use tape diagrams/bar models, table of equivalent values, double number lines and equations to solve real world problems.	Bar Modeling (Google Doc) Please download into Word (picture is		nt or Activities: ontent-relate	CA Framework p. 9-13, 15-16 Flipbook p. 11-14 NC Unpacking p. 9-13
•	Which model makes the most sense to you? Why? How do you choose a	Jim and Jesse's Money Painting a Barn	3)	6.RP.3 Make and manipulate tables of	rotated in Google – it will correct in Word) Equations with rate		asks for early nishers Game	 <u>Alignment for outcomes 2 & 3</u> enVision, Topic 9: Lesson 9-2 – "Equivalent Ratios" Lesson 9-3 – "Modeling Ratios"
	model that is appropriate for solving a problem?	Running at a Constant Speed	2)	equivalent ratios to solve real world problems paying special attention to the additive and multiplicative relationships within the table.	problems in 6 th grade should be treated as equivalent fraction problems. (p.19 - CA	0	Investigati on Partner Activity	
		<u>Gianna's Job</u>	4)	6.RP.3 Use tables of equivalent ratios to plot pairs of values on the coordinate plane to solve real world problems paying special attention to the	<u>Tables of equivalent</u> <u>ratios (Google Doc)</u>	Prom		<u>CA Framework</u> p. 9-13, 15-16 <u>Flipbook</u> p. 11-14 <u>NC Unpacking</u> p. 9-13

		Unit #2 Ratio and U	nit Rates		
Essential Questions	Assessments for Learning	Sequence of Learning Outcomes 6.RP.1, 6.RP.2, 6.RP.3	Strategies for Teaching and Learning	Differentiation (EL/SpEd/GATE)	Resources
 For Learning Outcomes 5-7: How do you find unit rate if it's not given to you? When creating a unit rate, which quantity do you want the 1 in the unit rate to be? 	For Learning Outcomes 6-7: From Illustrative Mathematics: Running at a Constant Speed, Assessment Variation Friends Meeting on Bicycles	 unit rate, including those with constant speed, with a variety of models. Discuss the meaning and usefulness of unit rate when solving problems. 6.RP.2 and 6.RP.3 7) Solve real-world problems by first finding the unit rate with a variety of models, in particular tables and 	Coordinate plane – pre-slope Address unit rate as per 1 and as 1 per, e.g. For speed, how many miles can be driven in one hour and how long does it take to drive one mile.	 Language of the Discipline Patterns Unanswer ed Questions Rules Trends Big Ideas Complexit y Differentiation Resources from <u>SCUSD</u> Wikispace:	Flipbook p. 11-14 NC Unpacking p. 9-13 enVision, Topic 10: • Lesson 10-2 – "Comparing Rates"
	Price per Pound and Pounds per Dollar	double number lines. Include problems of unit pricing to find the best value. 6.RP.2 and 6.RP.3			 enVision, Topic 10: Lesson 10-3 – "Unit Rates" Lesson 10-4 – "Unit Price"

			Unit #2 Ratio and U	nit Rates		
	Essential Questions	Assessments for Learning	Sequence of Learning Outcomes 6.RP.1, 6.RP.2, 6.RP.3	Strategies for Teaching and Learning	Differentiation (EL/SpEd/GATE)	Resources
•	What's the connection between percentages, rates, fractions and decimals?	For Learning Outcomes 8-10: From Illustrative Mathematics: <u>"Overlapping Squares"</u> <u>"Shirt Sale"</u>	 8) Represent percents as a rate per 100. Compare values written as fractions, decimals and percents. Use double number lines and unit rate reasoning to reinforce the idea that percents are per 100 and to solve percent problems. 6.RP.3 	development: <u>Converting Between a</u> <u>Decimal, Fraction, and</u> <u>Percentage</u>		 CA Framework p. 17-20 Flipbook p. 10-14 NC Unpacking p. 9-13 enVision, Topic 11: Lesson 11-1 – "Understanding Percent" Lesson 11-2 – "Fractions, Decimals , and Percents"
•	How and why do we use benchmark percentages?		 9) Recognize benchmark percentages (1%, 10%, 25%, 50%) as a fraction of 100%. 6.RP.3 			 <u>CA Framework</u> p.17-20 <u>Flipbook</u> p. 11-14 <u>NC Unpacking</u> p. 9-13 enVision, Topic 11: Lesson 11-4 – "Estimating Percent" Lesson 11-5 – "Finding the Percent of a Number" Lesson 11-7 – "Reasonableness"
•	What does a percentage more than 100% mean? How is a percentage greater than 100% different from a percentage less than 100%?		 10) Solve percentage problems involving unknown part, unknown percentage and unknown whole using a variety of strategies. (Framework p.18) 6.RP.3 	greater than 100%.		 <u>CA Framework</u> p. 17-20 <u>Flipbook</u> p. 11-14 <u>NC Unpacking</u> p. 9-13 <u>enVision, Topic 11:</u> Lesson 11-3 – "Percents Greater Than 100 or Less Than 1" Lesson 11-6 – "Finding the Whole" Reteaching Set C, p. 306

Unit #3: Algebraic Expressions

(Approx. # of Days 24-30)

6.EE.1-4

In this unit, students will be able to use, create, and compare expressions.

Common Core State Standards-Mathematics:

Expressions and Equations 6.EE

Apply and extend previous understandings of arithmetic to algebraic expressions.

- 1. Write and evaluate numerical expressions involving whole-number exponents.
- 2. Write, read, and evaluate expressions in which letters stand for numbers.
 - a. Write expressions that record operations with numbers and with letters standing for numbers. For example, express the calculation "Subtract y from 5" as 5 y.
 - b. Identify parts of an expression using mathematical terms (sum, term, product, factor, quotient, coefficient); view one or more parts of an expression as a single entity. For example, describe the expression 2 (8 + 7) as a product of two factors; view (8 + 7) as both a single entity and a sum of two terms.
 - c. Evaluate expressions at specific values of their variables. Include expressions that arise from formulas used in real-world problems. Perform arithmetic operations, including those involving whole-number exponents, in the conventional order when there are no parentheses to specify a particular order (Order of Operations). For example, use the formulas $V = s^3$ and $A = 6 s^2$ to find the volume and surface area of a cube with sides of length s = 1/2.
- 3. Apply the properties of operations to generate equivalent expressions. For example, apply the distributive property to the expression 3 (2 + x) to produce the equivalent expression 6 + 3x; apply the distributive property to the expression 24x + 18y to produce the equivalent expression 6 (4x + 3y); apply properties of operations to y + y + y to produce the equivalent expression 3y.
- 4. Identify when two expressions are equivalent (i.e., when the two expressions name the same number regardless of which value is substituted into them). For example, the expressions y + y + y and 3y are equivalent because they name the same number regardless of which number y stands for.

Standards for Mathematical Practice:

- SMP.1 Make sense of problems and persevere in solving them
- SMP.2 Reason abstractly and quantitatively
- SMP.3 Construct viable arguments and critique the reasoning of others
- SMP.4 Model with mathematics
- SMP.6 Attend to precision.

ELD Standards to Support Unit

Part I: Interacting in Meaningful Ways:

G. Collaborative:

4. Interacting with others in written English in various communicative forms

8. Adapting language choices to various contexts

H. Interpretive:

- 9. Listening actively to spoken English in a range of social and academic contexts.
- I. Productive:

11. Supporting own opinions and evaluating others' opinions in speaking and writing.

- Part II: Learning About How English Works
- Expanding and Enriching Ideas
 - 5. Modifying to add details.
- Connecting and Condensing Ideas
 - 6. Connecting Ideas
 - 7. Condensing Ideas

Self-awareness

Self-management

Social awareness

Relationship skills

Responsible decision making

		Unit #3 Algeb	raic Expressions		
Essential Questions	Assessments for Learning	Sequence of Learning Outcomes 6.EE.1, 6.EE.2, 6.EE.3, 6.EE.4	Strategies for Teaching and Learning	Differentiation (EL/SpEd/GATE)	Resources
Essential Questions are thought- provoking, open-ended questions to be used within daily lessons that and are therefore connected to the Sequence of Learning Outcomes	Assessments for Learning address Diagnostic, Formative, and Summative assessments used throughout the unit to inform instruction connected to the Sequence of Learning Outcomes. <i>Note: These assessments are suggested, not required.</i>	Sequence of Learning Outcomes is intentionally organized for student success. Each outcome is not necessarily intended to be taught within one class session. Each Outcome begins with Students will be able to	 Strategies to support Unit: From the CA Mathematics <i>"Instructional Strategies"</i> chapter provides research-based strategies for teaching math, K-12 <i>"Supporting High Quality</i> Common Core Instruction" chapter addresses the development, implementation, and maintenance of high-quality, standards-based mathematics instructional programs <i>"Universal Design for Learning"</i> from CAST, the Center for Applied Special Technology 	Differentiation support for Unit: Use of math journals for differentiation and formative assessment. See <u>Teaching Channel</u> Video Flexible grouping: • Content • Interest • Project/product • Level (Heterogeneous/ Homogeneous) Tiered: 5. Independent Management Plan (Must Do/May Do) 6. Grouping • Content • Rigor w/in the concept • Project-base d learning	 CCSS Support for the Unit: CA Mathematics Framework Gr. 6 p. 1-6 "What Students Learn in Grade 5" p. 37-41 Expressions and Equations Progressions for CCSS-M Narrative documents describing the progression of a topic across a number of grade levels, informed both by research on children's cognitive development and by the logical structure of mathematics. Progressions on Expressions and Equations Overview p. 2-3 Grade 6 p. 4-6 Kansas Association of Teachers of Mathematics (KATM) 6th Grade Flipbook Provide illustrated examples, instructional strategies, additional resources/tools and misconceptions by standard. p. 34 - 40 North Carolina Department of Public Instructional strategies, additional resources/tools and misconceptions by standard. P. 34 - 40

			Unit #3 Algebr	aic Expressions		
Essential	Questions	Assessments for Learning	Sequence of Learning Outcomes 6.EE.1, 6.EE.2, 6.EE.3, 6.EE.4	Strategies for Teaching and Learning	Differentiation (EL/SpEd/GATE)	Resources
What does	s x⁵ mean?	For Learning Outcome 1: From Illustrative Mathematics: " <u>The Djinni's Offer</u> " <u>"Seven to the What???"</u> "Sierpinski's Carpet"	 Express any term of the form xⁿ as n factors of x (e.g. 4³ = 4.4.4). Evaluate terms of the form xⁿ as the product of n factors in real-world and mathematical contexts. The base(s) should be whole numbers, positive decimals or positive fractions. 6.EE.1 	Compare and contrast the meaning of 4(3) as the sum of 4 terms of 3 (3 + 3 + 3 + 3) and 4^3 as the product of 3 factors of 4 (4·4·4) – (emphasize difference - repeated addition for multiplication vs. exponents for repeated multiplication)	 Homework Grouping Formative Assessment Anchor Activities: Content-related Tasks for early finishers Game 	CA Framework p.37-38 Progressions p. 2-4 Flipbook p. 34-35 NC Unpacking p. 29 enVision, Topic 1: • Lesson 1-1 – "Exponents"
 the order i simplify an How do yo terms in ar What is the 	ou determine in which you n expression? ou identify the n expression? e difference an expression uation?	For Learning Outcome 2: From Illustrative Mathematics: " <u>Watch Out for</u> <u>Parentheses</u> " <u>"Distance to School"</u>	 2) Evaluate numerical expressions with exponents, factors and terms by identifying the structure of the expression: simplify the exponents, factors, then the terms. 6.EE.1 and 6.EE.2 	From SCUSD resource development: For learning experience 2 - <u>Google Doc</u> Notice that PEMDAS was not used here, because students may develop misconceptions when using PEMDAS. For example, student always multiplies before dividing.	 Game Investigation Partner Activity Stations Depth and Complexity Prompts/Icons: Depth Canguage of 	CA Framework p.38-40 Progressions p. 2-6 Flipbook p. 36-37 NC Unpacking p. 30-33 enVision, Topic 1: • Lesson 1-3 – "Order of Operations" • Lesson 1-5 – "Evaluating Numerical Expressions"
ways to re multiplicat	present tion? : we use x as a	For Learning Outcome 3: From Illustrative Mathematics: <u>"Rectangle Perimeter"</u> <u>"SCUSD Wikispace –</u> <u>6.EE.1-8 Assessments</u> " p. 3-7	 3) Translate the expression into words, given an expression with one of the four operations, including at least one variable, (5 – y describes subtracting y from 5). Also, given a description in words, write an appropriate mathematical expression. 6.EE.2 	Have the students use terms, some with variables to create simple expressions and find multiple ways to combine them. (i.e. 5, 3y, & 4m can be added, multiplied, divided, subtracted, used as exponents, etc. in multitude of ways). They can then practice the standard through this method.	 b Language of the Discipline o Patterns o Unanswered Questions o Rules o Trends o Big Ideas o Complexity 	 <u>CA Framework p. 38-40</u> <u>Progressions p. 2-6</u> <u>Flipbook p. 36-37</u> <u>NC Unpacking p. 30-33</u> enVision, Topic 1: Lesson 1-6 – "Using Variables to Write Expressions"

		Unit #3 Algeb	raic Expressions		
Essential Questions	Assessments for Learning	Sequence of Learning Outcomes 6.EE.1, 6.EE.2, 6.EE.3, 6.EE.4	Strategies for Teaching and Learning	Differentiation (EL/SpEd/GATE)	Resources
 Why is 3x + 2 not equal to 5x? Why is 2x + 3x not equal to 5x²? 	For Learning Outcome 4-5: From Illustrative Mathematics: <u>"Rectangle Perimeter 2"</u>		Combining like terms using the commutative and associative properties Learn Zillion Video Common Misconceptions Students may have when combining terms: 3x + 2y = 5xy $5x^2 + 6x^4 = 11x^6$ 3x + 5x + x = 8x	Resources from SCUSD Wikispace:	 <u>CA Framework p.40-41</u> <u>Progressions p. 2-3 & 6</u> <u>Flipbook p. 39-40</u> <u>NC Unpacking p. 34-35</u> <u>enVision, Topic 1:</u> Lesson 1-10 – "Simplifying Algebraic Expressions" Lesson 1-11 – Writing Algebraic Expressions" <u>CA Framework p. 40-41</u> <u>Progressions p. 2-3 & 6</u> <u>Flipbook p. 39-40</u> <u>NC Unpacking p. 34-35</u> <u>enVision, Topic 1:</u> Lesson 1-12 – "Equivalent Expressions"
 How do you identify the terms in an expression? 	From Project Paced <u>"Identify Parts of an</u> <u>Expression"</u> p. 5-6	describing each term using	Decompose each part of an expression into its base parts and recompose where appropriate. For example, describe the expression 2(8+7) as a product of two factors (2 and 15); view (8+7) as both a single entity		 <u>CA Framework</u> p. 38-40 <u>Progressions</u> p. 2-6 <u>Flipbook</u> p. 36-37 <u>NC Unpacking</u> p. 30-33 enVision, Topic 1: Lesson 1-7 – "Parts of an Expression"

		Unit #3 Algebi	raic Expressions		
Essential Questions	Assessments for Learning	Sequence of Learning Outcomes 6.EE.1, 6.EE.2, 6.EE.3, 6.EE.4	Strategies for Teaching and Learning	Differentiation (EL/SpEd/GATE)	Resources
 When evaluating the expression 4x for x = 5, why doesn't it create the number 45? What is the coefficient for x in the expression (2) 	For Learning Outcome 7: From Howard County Public School System: " <u>My First Fish Tank"</u> " <u>What's the Plan?"</u> For Learning Outcomes 8 –	(Framework – Examples of Expression Language pg. 39-40)	Learningand a sum of two terms.Focus on SMP 6 – "Attend to precision"Use the Assessment from Outcome 2 – "Distance to School" to begin substituting and decomposing – see solutions 1 and 2.Strategies for Outcomes 8-10:	(EL/SpEd/GATE)	CA Framework p.38-40 Progressions p. 2-6 Flipbook p. 36-37 NC Unpacking p. 30-33 enVision, Topic 1: • Lesson 1-7 – "Parts of an Expression" • Problem Solving p.23 CA Framework p.38-41 Progressions p. 2-6
 + x)? Explain why 5(6 + 3x) is equal to 30 + 15x? How do you determine if two or more expressions are equivalent? Why does substituting a value not always work for determining equivalence of expressions? 	From Mathematics Assessment Project: " <u>Expressions and Areas</u> " From Illustrative Mathematics: " <u>Rectangle Perimeter 3</u> " " <u>Equivalent Expressions</u> "	 factors 2(15) and as a sum of terms (8+7) + (8+7). 6.EE.2 and 6.EE.3 9) Use the sum of terms (learning outcome 7) to rewrite 2(8+7) as (8+7) + (8+7) and then regroup into (8+8) + (7+7) for the purpose of discovering the distributive property 2(8) + 2(7). 6.EE.2 and 6.EE.3 10) Decompose an expression such as 2(3 + x) into (3+x)+(3+x) in order to regroup like terms (3+3)+(x+x) = 6 + 2x. Use this process to discover 	Visual model of the distributive property <u>Learn Zillion Video</u>		Flipbook p. 36-38NC Unpacking p. 30-34enVision, Topic 1:• Lesson 1-4 – "The Distributive Property"CA Framework p.38-41Progressions p. 2-6Flipbook p. 36-38NC Unpacking p. 30-34enVision, Topic 1:• Lesson 1-10 – "Simplifying Algebraic Expressions"CA Framework p.38-41Progressions p. 2-6Flipbook p. 36-38NC Unpacking p. 30-34

		Unit #3 Algebr	aic Expressions		
Essential Questions	Assessments for Learning	Sequence of Learning Outcomes 6.EE.1, 6.EE.2, 6.EE.3, 6.EE.4	Strategies for Teaching and Learning	Differentiation (EL/SpEd/GATE)	Resources
End of unit question that encompasses learning of entire unit: • What are all the ways you can write a given expression (such as 5x + 2y)?	For Learning Outcomes 8 – 12: From Mathematics Assessment Project: "Expressions and Areas" From Illustrative Mathematics: "Rectangle Perimeter 3" "Equivalent Expressions"	the short cut of multiplying by the coefficient (the distributive property). 6.EE.2 and 6.EE.3 11) Use previous learning experiences, the distributive property, and combining like terms to determine if two expressions are equivalent. (Example – Are the two following expressions equal? $5 n + 3 +$ 7n and 12n + 15 Justify your answer.) 6.EE.3 and 6.EE.4 12) Compare a given expression to multiple other expressions, to identify those that are equivalent and justify their reasoning using the structures of simplifying expressions including combining like terms and the distributive property. 6.EE.3 and 6.EE.4	As students are dealing with equivalent expressions, choosing numbers to plug in and test is wise. Use examples and assessments from outcomes 1-10 that students are already familiar with and revisit.		 enVision, Topic 1: Lesson 1-12 – "Equivalent Expressions" Symbolic Form Another Example Independent Practice CA Framework p.40-41 Progressions p. 2-3 & 6 Flipbook p. 38-40 NC Unpacking p. 33-35 enVision, Topic 1: Lesson 1-10 & Lesson 1-11 – "Simplifyin and Writing Algebraic Expressions" Independent Practice Problem Solving CA Framework p.40-41 Progressions p. 2-3 & 6 Flipbook p. 38-40 NC Unpacking p. 33-35 enVision, Topic 1: Lesson 1-2 - % Equivalent Expressions" Independent Practice Reteaching p. 41 Set L

Unit #4: Equations and Inequalities

(Approx. # of Days 32-40)

Content Standards: 6.EE.5-9

In this unit, students will be able to create, manipulate, and solve equations and inequalities

Common Core State Standards-Mathematics:

Expressions and Equations 6.EE

Reason about and solve one-variable equations and inequalities.

- 5. Understand solving an equation or inequality as a process of answering a question: which values from a specified set, if any, make the equation or inequality true? Use substitution to determine whether a given number in a specified set makes an equation or inequality true.
- 6. Use variables to represent numbers and write expressions when solving a real-world or mathematical problem; understand that a variable can represent an unknown number, or, depending on the purpose at hand, any number in a specified set.
- 7. Solve real-world and mathematical problems by writing and solving equations of the form x + p = q and px = q for cases in which p, q and x are all nonnegative rational numbers.
- 8. Write an inequality of the form *x* > *c* or *x* < *c* to represent a constraint or condition in a real-world or mathematical problem. Recognize that inequalities of the form *x* > *c* or *x* < *c* have infinitely many solutions; represent solutions of such inequalities on number line diagrams.

Represent and analyze quantitative relationships between dependent and independent variables.

9. Use variables to represent two quantities in a real-world problem that change in relationship to one another; write an equation to express one quantity, thought of as the dependent variable, in terms of the other quantity, thought of as the independent variable. Analyze the relationship between the dependent and independent variables using graphs and tables, and relate these to the equation. For example, in a problem involving motion at constant speed, list and graph ordered pairs of distances and times, and write the equation d = 65t to represent the relationship between distance and time.

Standards for Mathematical Practice:

SMP.3 – Construct viable arguments and critique the reasoning of others
 SMP.4 – Model with mathematics
 SMP.6 – Attend to precision.

Part I: Interacting in Meaningful Ways:	SEL Competencies:
 J. Collaborative: 5. Interacting with others in written English in various communicative forms 10. Adapting language choices to various contexts K. Interpretive: 11. Listening actively to spoken English in a range of social and academic contexts. L. Productive: 11. Supporting own opinions and evaluating others' opinions in speaking and writing. Part II: Learning About How English Works 	Self-awareness Self-management Social awareness Relationship skills Responsible decision making
 Expanding and Enriching Ideas 5. Modifying to add details. Connecting and Condensing Ideas 6. Connecting Ideas 7. Condensing Ideas 	

Unit #4 Equations and Inequalities					
Essential Questions	Assessments for Learning	Sequence of Learning Outcomes 6.EE.5-9	Strategies for Teaching and Learning	Differentiation (EL/SpEd/GATE)	Resources
Essential Questions are thought- provoking, open-ended questions to be used within daily lessons that and are therefore connected to the Sequence of Learning Outcomes	Assessments for Learning address Diagnostic, Formative, and Summative assessments used throughout the unit to inform instruction connected to the Sequence of Learning Outcomes. <i>Note: These assessments are suggested, not required.</i>	Sequence of Learning Outcomes is intentionally organized for student success. Each outcome is not necessarily intended to be taught within one class session. Each Outcome begins with Students will be able to	 Strategies to support Unit: From the CA Mathematics Framework <u>"Instructional Strategies"</u> chapter provides research-based strategies for teaching math, K-12 <u>"Supporting High Quality</u> <u>Common Core Instruction"</u> chapter addresses the development, implementation, and maintenance of high-quality, standards-based mathematics instructional programs <u>"Universal Design for Learning"</u> from CAST, the Center for Applied Special Technology 	Differentiation support for Unit: Use of math journals for differentiation and formative assessment. See <u>Teaching Channel</u> Video Flexible grouping: • Content • Interest • Project/product • Level (Heterogeneous/ Homogeneous) Tiered: 13) Independent Management Plan (Must Do/May Do) 14) Grouping a. Content b. Rigor w/in the concept C. Project-bas ed learning d. Homework e. Grouping <i>f.</i> Formative Assessmen	 CCSS Support for the Unit: CA Mathematics Framework Gr. 6 p. 1-6 "What Students Learn in Grade 5" p. 42-46 Expressions and Equations Progressions for CCSS-M Narrative documents describing the progression of a topic across a number of grade levels, informed both by research on children's cognitive development and by the logical structure of mathematics. Progressions on Expressions and Equations Overview p. 2-3 Grade 6 p. 4 & 6-7 Kansas Association of Teachers of Mathematics (KATM) 6th Grade Flipbook Provide illustrated examples, instructional strategies, additional resources/tools and misconceptions by standard. p. 39 - 49 North Carolina Department of Public Instructional strategies, additional resources/tools and miscructional strategies, additional resources/tools and miscructional strategies, additional resources/tools and miscructional strategies, additional resources/tools and misconceptions by standard. p. 39 - 49 North Carolina Department of Public Instruction: Unpacked Content Provides illustrated examples, instructional strategies, additional resources/tools and miscructional strategies, additional resources/tools and Provides illustrated examples, Provides and Provides and Pr

	Unit #4 Equations and Inequalities				
Essential Questions	Assessments for Learning	Sequence of Learning Outcomes 6.EE.5-9	Strategies for Teaching and Learning	Differentiation (EL/SpEd/GATE)	Resources
 What's the difference between an expression and an equation? What's the difference between a situation represented by x + p and one represented by px? 	Assessments/Tasks aligned to learning outcomes: Note: These Assessments are suggested, not required. Learning Outcomes 1 – 5: From SCUSD Resource Development: <u>Party Planning</u> From Illustrative Mathematics: <u>"Firefighter Allocation"</u> <u>"Triangular Tables"</u>	 Students will be able to 1) Represent real-world situations by writing expressions of the form x + p. Clearly define the meaning of the variable and the expression. Framework p.42. 	Learning outcomes 1 and 2 should focus only on writing and representing expressions (no equality) with mathematical symbols and bar models. Videos of using tape diagrams for representing expressions and solving equations: From Learn Zillion: <u>Solving equations with addition</u> <u>Solving equations with subtraction</u>	t Anchor Activities: • Content-related • Tasks for early finishers • Game • Investigation • Partner Activity • Stations Depth and Complexity	 misconceptions by standard. P. 36-42 <i>Expressions and Equations</i> CA Framework p.38-41 Progressions p. 7 Flipbook p. 43 NC Unpacking p. 37-39 enVision Topic 1: Lesson 1-6 – "Using Variables to Write Expressions" CA Framework p.38-41 Progressions p. 7 Flipbook p. 43 NC Unpacking p. 37-39 enVision Topic 4: Lesson 4-6 – "Make a Table and Look for a Pattern"
 What's the difference between an expression and an equation? 	<u>"Busy Day"</u>	 6.EE.6 3) Write equations in the form x + p = q and create bar models to represent real-world situations. Clearly define the meaning of the variable and the both 	Solving equations with division From Vimeo:	 Complexity Differentiation Resources from <u>SCUSD Wikispace:</u> 	CA Framework p.38-41 Progressions p. 4 & 7 Flipbook p. 44-45 NC Unpacking p. 39-40
 How are bar models used to solve equations? 		expressions in the equations. 6.EE.7	Note that bar modeling should be used as a tool to build the concept	Differentiation support for Unit:	 enVision Topic 4: Lesson 4-3 – "Solving Addition

	Unit #4 Equations and Inequalities					
Essent	tial Questions	Assessments for Learning	Sequence of Learning Outcomes 6.EE.5-9	Strategies for Teaching and Learning	Differentiation (EL/SpEd/GATE)	Resources
 used dispr Whice operation zeroe invertion creation Whice you use equation 	r is substitution I to prove or rove an answer? ch inverse rations create es? Which rse operations te 1's? ch strategies can use to solve ations? When are appropriate?		 4) Solve equations of the form x + p = q using bar models and tables to facilitate guess and check. Use substitution to prove that a solution makes the equation true. 5) Solve equations of the form x + p = q using inverse operations. Use substitution to prove that a solution makes the equation true. 6.EE.5 and 6.EE.7 	whole numbers From SCUSD resource development: Bar Modeling (Google Doc) Guess and Check Tables (Google Doc)	Use of math journals for differentiation and formative assessment. See <u>Teaching Channel</u> <u>Video</u> Flexible grouping: Content Interest Project/product Level (Heterogeneous/ Homogeneous) Tiered: 15) Independent Management Plan (Must Do/May Do)	and Subtraction Equations" Alignment for Outcomes 4 & 5: CA Framework p.38-41 Progressions p. 4 & 7 Flipbook p. 41-42 & 44-45 NC Unpacking p. 36-37 & 39-40 enVision Topic 2: • Lesson 2-1 – "Understanding Equations" • Lesson 2-3 – "Solving Addition and Subtraction Equations"
betw expre	veen an ression and an ation?	Learning Outcomes 6 – 12: From Math Assessment Resource Service: <u>"Real Life Equations"</u> From SCUSD resource development: " <u>Cookies Galore"</u> From Illustrative Mathematics:	 6) Represent real-world situations by writing expressions of the form px. Clearly define the meaning of the variable and the expression. Framework p.42. 6.EE.6 7) Write and evaluate expressions representing real-world situations, of the form px, for multiple values of the variable. Use bar models and numeric 	In px = q, keep in mind that p, x and q are rational numbers but student work should begin with whole numbers. When solving equations in the form px = q, students should be exposed to inverse operation as both dividing by p and as multiplying by the reciprocal of p. Students need to understand the connection between both and should be able to identify	ed learning	 Alignment for Outcomes 6 & 7: <u>CA Framework p.38-41</u> <u>Progressions p. 7</u> <u>Flipbook p. 43</u> <u>NC Unpacking p. 37-39</u> enVision, Topic 2: Lesson 2-9 – "Draw a Picture and Write an Equation"

	Unit #4 Equations and Inequalities					
	Essential Questions	Assessments for Learning	Sequence of Learning Outcomes 6.EE.5-9	Strategies for Teaching and Learning	Differentiation (EL/SpEd/GATE)	Resources
•	 What's the difference between an expression and an equation? In solving px = q, how are multiplying by the reciprocal of p and dividing by p related? How are bar models used to solve equations? How is substitution used to prove or disprove an answer? Which inverse operations create 	"Pennies to Heaven" "Morning Walk" "Anna in D.C."	representations. Define the meaning of the variable and expression. 6.EE.6 8) Write equations in the form px = q and create bar models to represent real-world situations. Clearly define the meaning of the variable and the both expressions in the equations. 6.EE.5 and 6.EE.7 9) Solve equations of the form px = q using bar models and tables to facilitate guess and check. Use substitution to prove that a solution makes the equation true. 6.EE.5 and 6.EE.7	when it is easiest to use each operation. In px = q, keep in mind that p, x and q are rational numbers but student work should begin with whole numbers When solving equations in the form px = q, students should be exposed to inverse operation as both dividing by p and as multiplying by the reciprocal of p. Students need to understand the connection between	 Anchor Activities: Content-related Tasks for early finishers Game Investigation Partner Activity Stations Depth and Complexity Prompts/Icons: Depth Language of the Discipline Patterns Unanswered Questions Rules Trends Big Ideas Complexity 	Alignment for Outcomes 8 & 9: CA Framework p.38-41 Progressions p. 4 & 6-7 Flipbook p. 41-42 & 44-45 NC Unpacking p. 36-37 & 39-40 enVision, Topic 2: • Lesson 2-4 – "Draw a Picture and Write an Equation" • Lesson 2-5 – " Solving Multiplication and Division Equations"
	 zeroes? Which inverse operations create 1's? (What do we mean by zeroes and ones?) Which strategies can you use to solve equations? When are 		 10) Solve equations of the form px = q using inverse operations, where p is a whole number and then a fraction. Use substitution to prove that a solution makes the equation true. 6.EE.5 and 6.EE.7 	both and should be able to identify when it is easiest to use each operation.	Differentiation Resources from <u>SCUSD Wikispace</u> :	Alignment for Outcomes 10 - 12: <u>CA Framework</u> p.38-41 <u>Progressions</u> p. 4 & 6-7 <u>Flipbook</u> p. 41-42 & 44-45 <u>NC Unpacking</u> p. 36-37 & 39-40

	Unit #4 Equations and Inequalities				
Essential Questions	Assessments for Learning	Sequence of Learning Outcomes 6.EE.5-9	Strategies for Teaching and Learning	Differentiation (EL/SpEd/GATE)	Resources
they appropriate?		 11) Solve equations of the form px = q using inverse operations, where p is a decimal. Use substitution to prove that a solution makes the equation true. 6.EE.5 and 6.EE.7 12) Distinguish between real-world situations represented by p + x = q and px = q, solving problems of each type using inverse operations. 6.EE.7 			 enVision, Topic 2: Lesson 2-6 – "Solving Equations with Fractions"
 How are equations and inequalities similar? Different? How are the solutions of equations and inequalities different? 	For Learning Experiences 13 & 14: From SCUSD resource development: " <u>Hershey Park Inequalities"</u> From Illustrative Mathematics: " <u>Fishing Adventures 1"</u> " <u>Log Ride"</u> From Inside Mathematics: <u>"Boxes"</u>	 13) Write inequalities to represent real-world situations and identify possible solutions, recognizing that there can be infinitely many solutions. 6.EE.5 and 6.EE.8 14) Represent inequalities on a number line numerically and in real-world situations, representing constraints appropriately. (Framework p. 44) 6.EE.5 and 6.EE.8 	Outcomes 13 and 14 involve inequalities represented by the symbols > and < only. Students should make sense of why an open circle is used to represent that the boundary number is not a solution to the inequality.		 Alignment for Outcomes 13 & 14: CA Framework p.38-41 Progressions p. 6-7 Flipbook p. 41-42 & 46 NC Unpacking p. 36-37 & 40-41 enVision, Topic 2: Lesson 2-7 – "Writing Inequalities" Lesson 2-8 – "Solving Inequalities"

Unit #4 Equations and Inequalities							
Essential Questions	Assessments for Learning	Sequence of Learning Outcomes 6.EE.5-9	Strategies for Teaching and Learning	Differentiation (EL/SpEd/GATE)	Resources		
dependent? Independent? In the coordinate plane, which axis goes with the independent variable? The dependent variable?	For Learning Experiences 15-18: From Illustrative Mathematics: "Chocolate Bar Sales" From Inside Mathematics: "Gym"		Outcomes 15 – 18 may be taught concurrently rather than as distinct learning experiences in order to relate the situation, table, graph, and equation of a given real-world problem. The use of multiple representations simultaneously is key here. Translating between multiple representations helps students understand that each form represents the same relationship and provides different perspective on the relationship.		 <u>CA Framework p.38-41</u> <u>Progressions p. 7</u> <u>Flipbook p. 47-49</u> <u>NC Unpacking p. 42</u> enVision, Topic 3: Lesson 3-1 – "Dependent and Independent Variables" <u>CA Framework p.38-41</u> <u>Progressions p. 7</u> <u>Flipbook p. 47-49</u> <u>NC Unpacking p. 42</u> enVision, Topic 3: Lesson 3-2 – "Patterns and Equations" enVision, Topic 4: Lesson 4-6 - "Make a Table and Look for a Pattern" 		

	Unit #4 Equations and Inequalities							
Essential Questions	Assessments for Learning	Sequence of Learning Outcomes 6.EE.5-9	Strategies for Teaching and Learning	Differentiation (EL/SpEd/GATE)	Resources			
	For Learning Experiences 15-18: From Illustrative Mathematics: <u>"Chocolate Bar Sales"</u> From Inside Mathematics: <u>"Gym"</u>	context of the problem.	Outcomes 15 – 18 may be taught concurrently rather than as distinct learning experiences in order to relate the situation, table, graph, and equation of a given real-world problem. The use of multiple representations simultaneously is key here. Translating between multiple representations helps students understand that each form represents the same relationship and provides different perspective on the relationship.		 Alignment for Outcomes 17 & 18: CA Framework p.38-41 Progressions p. 7 Flipbook p. 47-49 NC Unpacking p. 42 enVision, Topic 3: Lesson 3-3 – "More Patterns and Equations" enVision, Topic 10: Lesson 10-5 – "Constant Speed" 			

Unit #5: Rational Numbers

(Approx. # of Days 15-22)

Content Standards: 6.NS.5-8

In this unit, students will be able to use integers and rational numbers (including absolute value) on a number line and a coordinate plane.

Common Core State Standards-Mathematics:

Number System 6.NS

Apply and extend previous understandings of numbers to the system of rational numbers.

- 5. Understand that positive and negative numbers are used together to describe quantities having opposite directions or values (e.g., temperature above/below zero, elevation above/below sea level, credits/debits, positive/negative electric charge); use positive and negative numbers to represent quantities in real-world contexts, explaining the meaning of 0 in each situation.
- 6. Understand a rational number as a point on the number line. Extend number line diagrams and coordinate axes familiar from previous grades to represent points on the line and in the plane with negative number coordinates.
 - a. Recognize opposite signs of numbers as indicating locations on opposite sides of 0 on the number line; recognize that the opposite of the opposite of a number is the number itself, e.g., -(-3) = 3, and that 0 is its own opposite.
 - b. Understand signs of numbers in ordered pairs as indicating locations in quadrants of the coordinate plane; recognize that when two ordered pairs differ only by signs, the locations of the points are related by reflections across one or both axes.

c. Find and position integers and other rational numbers on a horizontal or vertical number line diagram; find and position pairs of integers and other rational numbers on a coordinate plane. 7. Understand ordering and absolute value of rational numbers.

- a. Interpret statements of inequality as statements about the relative position of two numbers on a number line diagram. For example, interpret –3 > –7 as a statement that –3 is located to the right of
 - -7 on a number line oriented from left to right.
 - b. Write, interpret, and explain statements of order for rational numbers in real-world contexts. For example, write $-3^{\circ}C > -7^{\circ}C$ to express the fact that $-3^{\circ}C$ is warmer than $-7^{\circ}C$.
 - c. Understand the absolute value of a rational number as its distance from 0 on the number line; interpret absolute value as magnitude for a positive or negative quantity in a real-world situation. For example, for an account balance of -30 dollars, write |-30| = 30 to describe the size of the debt in dollars.
 - d. Distinguish comparisons of absolute value from statements about order. For example, recognize that an account balance less than -30 dollars represents a debt greater than 30 dollars.
- 8. Solve real-world and mathematical problems by graphing points in all four quadrants of the coordinate plane. Include use of coordinates and absolute value to find distances between points with the same first coordinate or the same second coordinate.

Standards for Mathematical Practice:

- SMP.1 Make sense of problems and persevere in solving them
- SMP.2 Reason abstractly and quantitatively
- SMP.4 Model with mathematics

ELD Standards to Support Unit:

Part I: Interacting in Meaningful Ways:

- M. Collaborative:
 - 6. Interacting with others in written English in various communicative forms
 - 12. Adapting language choices to various contexts
- N. Interpretive:
 - 13. Listening actively to spoken English in a range of social and academic contexts.
- O. Productive:
 - 11. Supporting own opinions and evaluating others' opinions in speaking and writing.

Part II: Learning About How English Works

- Expanding and Enriching Ideas
 - 5. Modifying to add details.
- Connecting and Condensing Ideas
 - 6. Connecting Ideas
 - 7. Condensing Ideas

SEL Competencies:

Self-awareness

Self-management

Social awareness

Relationship skills

Responsible decision making

Unit #5 Rational Numbers						
Essential Questions	Assessments for Learning	Sequence of Learning Outcomes 6.NS.5, 6.NS.6, 6.NS.7, 6.NS.8	Strategies for Teaching and Learning	Differentiation (EL/SpEd/GATE)	Resources	
Essential Questions are thought- provoking, open-ended questions to be used within daily lessons that and are therefore connected to the Sequence of Learning Outcomes	Assessments for Learning address Diagnostic, Formative, and Summative assessments used throughout the unit to inform instruction connected to the Sequence of Learning Outcomes. <i>Note: These assessments are suggested, not required.</i>	Sequence of Learning Outcomes is intentionally organized for student success. Each outcome is not necessarily intended to be taught within one class session. Each Outcome begins with Students will be able to	Strategies to support Unit: From the CA Mathematics Framework • <u>"Instructional Strategies"</u> chapter provides research-based strategies for teaching math, K-12 • <u>"Supporting High Quality</u> <u>Common Core Instruction"</u> chapter addresses the development, implementation, and maintenance of high-quality, standards-based mathematics instructional programs <u>"Universal Design for</u> <u>Learning"</u> from CAST, the Center for Applied Special Technology	Differentiation support for Unit: Use of math journals for differentiation and formative assessment. See <u>Teaching Channel</u> Video Flexible grouping: • Content • Interest • Project/product • Level (Heterogeneous/ Homogeneous) Tiered: 17) Independent Management Plan (Must Do/May Do) 18) Grouping a. Content b. Rigor w/in the concept c. Project-ba sed learning d. Homewor k	instructional strategies, additional resources/tools and misconceptions by standard. p. 24 – 33 Number Sense <u>North Carolina Department of Public</u> <u>Instruction: Unpacked Content</u>	

	Unit #5 Rational Numbers							
Essential Questions	Assessments for Learning	Sequence of Learning Outcomes 6.NS.5, 6.NS.6, 6.NS.7, 6.NS.8	Strategies for Teaching and Learning	Differentiation (EL/SpEd/GATE)	Resources			
 What is the relationship between positive and negative numbers? Is zero positive or negative? Explain. Where do we see negative numbers in the real world? What are rational numbers? How do you use a number line to represent magnitude of a number? Why are bigger negative numbers really smaller? What does it mean for numbers to be opposites? 	From Illustrative Mathematics: <u>Mile High</u> <u>Fractions on a Number Line</u> From Common Core Toolbox: <u>Cake Weighing</u>	 Make sense of positive and negative rational numbers in context of a real-world situation, explaining the meaning of zero in each situation. 6.NS.5 Plot rational numbers on number lines, both horizontal and vertical, in context of a real-world situation such as temperature or elevation. 6.NS.6 Understand positive and negative rational numbers as numbers on opposite sides of 0 on the number line, e. g(-3) as the opposite of -3 otherwise known as 3. Graph opposites on a number line. 6.NS.6 	numbers refers more specifically to all positive and negative real numbers, including <u>but not limited to</u> integers. Note 2: Teachers should attend to precision in using the word "minus" only when referring to the operation of subtraction. Teachers should refer to numbers such as "-1/2" as negative one-half or the opposite of one-half. Real-world contexts for rational numbers: temperature, elevation, banking, electric charge	e. Grouping f. Formative Assessme nt Anchor Activities: Content-related Tasks for early finishers Game Investigation Partner Activity Stations Depth and Complexity Prompts/Icons: Depth Language of the Discipline Patterns Unanswered Questions Rules Trends Big Ideas Complexity Differentiation Resources from SCUSD Wikispace:	CA Framework p.31-35 Progressions p. 7 Flipbook p. 24 NC Unpacking p. 23 enVision, Topic 7: • Lesson 7-1 • Lesson 7-6 CA Framework p.31-35 Progressions p. 7-8 Flipbook p. 25-26 NC Unpacking p. 23-24 enVision, Topic 7: • Lesson 7-1 o "Guided Practice" - p. 184 • Lesson 7-4 o "Guided and Independent Practice" p. 192-3 CA Framework p.31-35 Progressions p. 7-8 Flipbook p. 25-26 NC Unpacking p. 23-24 enVision, Topic 7: • Lesson 7-1 o "Independent Practice" - p. 184			

	Unit #5 Rational Numbers						
Essential Questions	Assessments for Learning	Sequence of Learning Outcomes 6.NS.5, 6.NS.6, 6.NS.7, 6.NS.8	Strategies for Teaching and Learning	Differentiation (EL/SpEd/GATE)	Resources		
	 For Learning Outcomes 1 – 6: From SCUSD Resource Development: <u>Contest Winner</u> <u>Positive and negative events</u> <u>story</u> From Illustrative Mathematics: <u>Mile High</u> <u>Fractions on a Number Line</u> From Common Core Toolbox: <u>Cake Weighing</u> From IXL Math Online: <u>Put Rational Numbers In Order</u> From Engage NY: <u>Temperature - Exit Ticket pg. 41</u> 	 4) Graph all different types of rational numbers on the same number line, paying attention to the order of the numbers. 6.NS.6 5) Use number lines to make sense of relative size based on location, both in and out of real-world context, recognizing that a number to the right is always greater than a number to the left. 6.NS.6 		Differentiation support for Unit: Use of math journals for differentiation and formative assessment. See <u>Teaching Channel</u> Video Flexible grouping: • Content • Interest • Project/product • Level (Heterogeneous/ Homogeneous) Tiered: 19) Independent Management Plan (Must Do/May Do) 20) Grouping a. Content b. Rigor w/in the concept c. Project-ba sed	CA Framework p.31-35 Progressions p. 7-8 Flipbook p. 25-26 NC Unpacking p. 23-24 enVision, Topic 7: • Lesson 7-2 • p. 186-7 - Problems 9-11, 20-31, & 33 enVision, Topic 6: • Lesson 6-11 CA Framework p.31-35 Progressions p. 7-8 Flipbook p. 25-26 NC Unpacking p. 23-24 enVision, Topic 7: • Lesson 7-4 – • "Problem Solving" p. 194		

	Unit #5 Rational Numbers						
Essential Questions	Assessments for Learning	Sequence of Learning Outcomes 6.NS.5, 6.NS.6, 6.NS.7, 6.NS.8	Strategies for Teaching and Learning	Differentiation (EL/SpEd/GATE)	Resources		
 What is absolute value? When is absolute value used in the real world? 	For Outcomes 7 – 9: From Engage NY: Absolute Value (begins on pg. 98) From Illustrative Mathematics: Jumping Flea Above and Below Sea Level	 6) Write, interpret and explain inequality statements with rational numbers, using a number line to justify reasoning. 6.NS.7 7) Understand absolute value of a rational number as its distance from zero on a number line. 6.NS.7 8) Understand absolute value as magnitude for a positive or negative quantity in a real-world situation, e.g. owing 30 dollars represents the magnitude of -30 . 6.NS.7 		 learning Homewor Homewor Homewor Foruping Formative Assessme Assessme nt Anchor Activities: Content-related Tasks for early finishers Game Investigation Partner Activity Stations Depth and Complexity Prompts/Icons: Depth Language of the Discipline Patterns Unanswered Questions Rules Trends Big Ideas Complexity 	CA Framework p.35-37 Progressions p. 8 Flipbook p. 27-30 NC Unpacking p. 25-27 enVision, Topic 7: • Lesson 7-2 • P.186-7 – Problems 1-8, 12-19, & 32 Alignment for Outcomes 7-9: CA Framework p.35-37 Progressions p. 8 Flipbook p. 27-30 NC Unpacking p. 25-27 enVision, Topic 7: • Lesson 7-1 • "Problem Solving" problems 17-22 • Lesson 7-3		

		Unit #5 Ratio	onal Numbers		
Essential Questions	Assessments for Learning	Sequence of Learning Outcomes 6.NS.5, 6.NS.6, 6.NS.7, 6.NS.8	Strategies for Teaching and Learning	Differentiation (EL/SpEd/GATE)	Resources
		 9) Interpret absolute value inequality statements in real-world contexts. e.g. x > -10 may represent a debt greater than 10 dollars. 6.NS.7 		Differentiation Resources from <u>SCUSD Wikispace</u> :	
 What are the relationships between opposites on a coordinate plane? 	For Outcomes 10 – 12: From SCUSD Resource Development: <u>Amusement Park</u> From Internet for Classrooms:				Alignment for Outcomes 10 & 11: <u>CA Framework</u> p.31-37 <u>Progressions</u> p. 7-8 <u>Flipbook</u> p. 25-26 & 31-33 <u>NC Unpacking</u> p. 23-24 & 27-28
	<u>Coordinate Planes</u> From Khan Academy: <u>Coordinate Plane Word</u> <u>Problems</u>	coordinate pairs in each of the four quadrants of the coordinate plane, e.g. (-2, 0.75) must be in quadrant II because the x-coordinate is negative and the y-coordinate is positive. 6.NS.6 and 6.NS.8	<u>Coordinate Graphs Review</u> <u>Graph Points on a Coordinate</u>		 enVision, Topic 8: Lesson 8-1 Lesson 8-2
		 12) Recognize coordinate points with the same x- values and opposite y-values are reflections across the x-axis. Recognize coordinate points with the same y- values and opposite x-values are reflections across the y-axis. 6.NS.6 and 8 	From Internet 4 Classrooms: Coordinate Plane Material		CA Framework p.31-37 Progressions p. 7-8 Flipbook p. 25-26 & 31-33 NC Unpacking p. 23-24 & 27-28 enVision, Topic 8: • Lesson 8-3 • Lesson 8-4

Unit #6: Geometry
(Approx. # of Days 20-25)
Content Standards: 6.G.1-4, 6.NS.8
In this unit, students will be able to find the area and/or volume of multiple polygons through decomposition and to graph those polygons.
Common Core State Standards-Mathematics:
Geometry 6.G
Solve real-world and mathematical problems involving area, surface area, and volume.
1. Find the area of right triangles, other triangles, special quadrilaterals, and polygons by composing into rectangles or decomposing into triangles and other shapes; apply these techniques in the context of solving real-world and mathematical problems.
2. Find the volume of a right rectangular prism with fractional edge lengths by packing it with unit cubes of the appropriate unit fraction edge lengths, and show that the volume is the same as would be found by multiplying the edge lengths of the prism. Apply the formulas $V = I w h$ and $V = b h$ to find volumes of right rectangular prisms with fractional edge lengths in the context of solving real-world and mathematical problems.
3. Draw polygons in the coordinate plane given coordinates for the vertices; use coordinates to find the length of a side joining points with the same first coordinate or the same second coordinate. Apply these techniques in the context of solving real-world and mathematical problems.
4. Represent three-dimensional figures using nets made up of rectangles and triangles, and use the nets to find the surface area of these figures. Apply these techniques in the context of solving real-world and mathematical problems.
Number Sense 6.NS
Apply and extend previous understandings of numbers to the system of rational numbers.
8. Solve real-world and mathematical problems by graphing points in all four quadrants of the coordinate plane. Include use of coordinates and absolute value to find distances between points with the same first coordinate or the same second coordinate.
Standards for Mathematical Practice: SMP 3 – Construct viable arguments and critique the reasoning of others
SMP 4 – Model with mathematics
SMP 6 – Attend to precision
SMP 7 - Look for and make use of structure

ELD Standards to Support Unit:

Part I: Interacting in Meaningful Ways:

- P. Collaborative:
 - Interacting with others in written English in various communicative forms
 Adapting language choices to various contexts
- Q. Interpretive:
 - 15. Listening actively to spoken English in a range of social and academic contexts.
- R. Productive:

11. Supporting own opinions and evaluating others' opinions in speaking and writing.

Part II: Learning About How English Works

• Expanding and Enriching Ideas

5. Modifying to add details.

- Connecting and Condensing Ideas
 - 6. Connecting Ideas
 - 7. Condensing Ideas

Self-awareness

Self-management

Social awareness

Relationship skills

Responsible decision making

	Unit #6 Geometry							
Essential Questions	Assessments for Learning	Sequence of Learning Outcomes 6.G.1, 6.G.2, 6.G.3, 6.G.4, 6.NS.8	Strategies for Teaching and Learning	Differentiation (EL/SpEd/GATE)	Resources			
Essential Questions are thought- provoking, open-ended questions to be used within daily lessons that and are therefore connected to the Sequence of Learning Outcomes	Assessments for Learning address Diagnostic, Formative, and Summative assessments used throughout the unit to inform instruction connected to the Sequence of Learning Outcomes. <i>Note: These assessments are suggested, not required.</i>	Sequence of Learning Outcomes is intentionally organized for student success. Each outcome is not necessarily intended to be taught within one class session. Each Outcome begins with Students will be able to	 Strategies to support Unit: From the CA Mathematics Framework <u>"Instructional Strategies"</u> chapter provides research-based strategies for teaching math, K-12 <u>"Supporting High Quality</u> <u>Common Core Instruction"</u> chapter addresses the development, implementation, and maintenance of high-quality, standards-based mathematics instructional programs <u>"Universal Design for Learning"</u> from CAST, the Center for Applied Special Technology 	Differentiation support for Unit: Use of math journals for differentiation and formative assessment. See <u>Teaching Channel Video</u> Flexible grouping: • Content • Interest • Project/product • Level (Heterogeneous/ Homogeneous) Tiered: 21) Independent Management Plan (Must Do/May Do) 22) Grouping a. Content b. Rigor w/in the concept c. Project-base d learning d. Homework e. Grouping f. Formative	 CCSS Support for the Unit: <u>CA Mathematics Framework Gr. 6</u> p. 1-6 "What Students Learn in Grade 5" p. 46 -49 Geometry <u>Kansas Association of Teachers of</u> <u>Mathematics (KATM) 6th Grade</u> <u>Flipbook</u> Provide illustrated examples, instructional strategies, additional resources/tools and misconceptions by standard. p. 50-58 Geometry <u>North Carolina Department of Public</u> <u>Instruction: Unpacked Content</u> Provides illustrated examples, instructional strategies, additional resources/tools and misconceptions by standard. Provides illustrated examples, instructional strategies, additional resources/tools and misconceptions by standard. P. 43-49 Geometry 			

	Unit #6 Geometry							
Essential Questions	Assessments for Learning	Sequence of Learning Outcomes 6.G.1, 6.G.2, 6.G.3, 6.G.4, 6.NS.8	Strategies for Teaching and Learning	Differentiation (EL/SpEd/GATE)	Resources			
 What is area? What does it mean to derive a formula? Where do the formulas for triangles, parallelograms and trapezoids come from? How can you use decomposition to find the area of irregular shapes? How can the coordinate plane be used to help find area? 	From Illustrative Mathematics: <u>Painting a Barn</u> <u>Finding Areas of Polygons</u>	 Derive the area of a right triangle by decomposing the area of a rectangle into two congruent right triangles. 6.G.1 Derive the area of a parallelogram by decomposing and recomposing the parallelogram into a rectangle with congruent area. 6.G.1 	Derive the area of a right and non-right triangle. From Learn Zillion: Derive area of a parallelogram	Assessment Assessment Anchor Activities: Content-related Tasks for early finishers Game Investigation Partner Activity Stations Depth and Complexity Prompts/lcons: Depth Language of the Discipline Patterns Unanswered Questions	CA Framework p. 46-48 Flipbook p. 50-52 NC Unpacking p. 43-45 enVision, Topic 12: • Lesson 12-1 CA Framework p. 46-48 Flipbook p. 50-52 NC Unpacking p. 43-45 enVision, Topic 12: • Lesson 12-2			
		 3) Derive the area of non-right triangles by decomposing the area of a parallelogram into two congruent triangles. 6.G.1 4) Find area of triangles and parallelograms in mathematical and real-world contexts. 6.G.1 	<u>Derive the area of a right and</u> <u>non-right triangle.</u>	 Rules Trends Big Ideas Complexity Differentiation Resources from <u>SCUSD Wikispace:</u>	CA Framework p. 46-48Flipbook p. 50-52NC Unpacking p. 43-45enVision, Topic 12:• Lesson 12-3CA Framework p. 46-48Flipbook p. 50-52NC Unpacking p. 43-45			

	Unit #6 Geometry						
	Essential Questions	Assessments for Learning	Sequence of Learning Outcomes 6.G.1, 6.G.2, 6.G.3, 6.G.4, 6.NS.8	Strategies for Teaching and Learning	Differentiation (EL/SpEd/GATE)	Resources	
•	(recomposing, as opposed to decomposing) polygons to figure out the areas of more complex shapes? How can we estimate to figure out area while using irregular polygons?	From Illustrative Mathematics: Distances Between Points Polygons in the Coordinate Plane From HCPSS (Google Doc) For Outcome 8: Disaster at Sea • Supporting	 (0, 2) and (0, 0). 6.G.1, 6.G.3, & 6.NS.8 6) Find the area of isosceles trapezoids by decomposing into a rectangle and two congruent triangles. 6.G.1 7) Derive the area of any trapezoid by using an additional congruent trapezoid and creating a 	Strategies for Outcomes 6-8:	Differentiation support for Unit: Use of math journals for differentiation and formative assessment. See Teaching Channel Video Flexible grouping: • Content • Interest • Project/product • Level (Heterogeneous/ Homogeneous) Tiered: 23) Independent Management Plan (Must Do/May Do) 24) Grouping a. Content b. Rigor w/in the concept c. Project-base d learning d. Homework e. Grouping f. Formative Assessment	CA Framework p. 46-49 & 35-36 Flipbook p. 50-52, 55-56, & 31 NC Unpacking p. 43-45, 47-49, & 27-28 enVision, Topic 12: • Lesson 12-6 enVision, Topic 8: • Review Lessons 8-1 through 8-4 Alignment for Outcomes 6-8: CA Framework p. 46-48 Flipbook p. 50-52 NC Unpacking p. 43-45 enVision, Topic 12: • Lesson 12-4	
			parallelogram. 6.G.1		Assessment		

	Unit #6 Geometry						
Essential Questions	Assessments for Learning	Sequence of Learning Outcomes 6.G.1, 6.G.2, 6.G.3, 6.G.4, 6.NS.8	Strategies for Teaching and Learning	Differentiation (EL/SpEd/GATE)	Resources		
 How can a net be used to represent a three-dimensional figure? What is surface area? Why can you find surface area of a three-dimensional figure? How can a net be used to find surface area? 	For Outcomes 9-11: From HCPSS (Google doc): <u>Nets</u> <u>Prism Examples</u> <u>Does the Net</u> <u>Work?</u> From Illustrative Mathematics: <u>Nets for Pyramids and</u> <u>Prisms</u> <u>Computing Volume</u> <u>Progression 1</u> <u>Computing Volume</u> <u>Progression 2</u> <u>Computing Volume</u> <u>Progression 3</u> <u>Computing Volume</u> <u>Progression 4</u>	 8) Find the area of irregular polygons that can be decomposed into rectangles and triangles in both mathematical and real-world situations. 6.G.1 9) Create nets composed of rectangles and triangles to represent three-dimensional figures. Recognize which three-dimensional figure a net represents. 6.G.4 10) Use a net to find the surface area of a three-dimensional figure. 6.G.4 11) Find surface area of three-dimensional figures in real-world contexts. 	Strategies for Outcomes 9-11: From Learnzillion.com Identify different nets Surface area by using nets	Anchor Activities: • Content-related • Tasks for early finishers • Game • Investigation • Partner Activity • Stations Depth and Complexity Prompts/Icons: • Depth • Language of the Discipline • Patterns • Unanswered Questions • Rules • Trends • Big Ideas • Complexity Differentiation Resources from SCUSD Wikispace:	Alignment for Outcomes 9-11: CA Framework p. 46 & 49 Flipbook p. 57 NC Unpacking p. 49 enVision, Topic 12: • Lesson 12-7 enVision, Topic 13: • Lesson 13-1 • Lesson 13-2		

	Unit #6 Geometry							
	Essential Questions	Assessments for Learning	Sequence of Learning Outcomes 6.G.1, 6.G.2, 6.G.3, 6.G.4, 6.NS.8	Strategies for Teaching and Learning	Differentiation (EL/SpEd/GATE)	Resources		
• • • • •	What is volume? Why does volume have three dimensions? What is a unit cube? What is a 1/8 cubic inch? How does a $\frac{1}{n}x\frac{1}{n}x\frac{1}{n}$ cubic unit compare to a 1x1x1 cubic unit? How do you determine what size cubic unit to use for volume when the side lengths are fractional? What is the relationship between the two formulas we use for volume, V=bh and V=lwh? What does volume, stated in fractional cubes, mean about the size of the prism? What is the difference between saying the volume is $\frac{75}{8}in^3$ and the volume is 75 ($\frac{1}{8}$ cubic inches) How is volume represented in the real-world? What would $\frac{75}{8}in^3$ really mean?	For Outcomes 12-13: From Illustrative Mathematics: Banana Bread From Inside Mathematics: Building Blocks From HCPSS (Google Doc): Fish Are Fun	12) Find the volume of a right rectangular prism with fractional side lengths by first determining the appropriate $\frac{1}{n} \cdot \frac{1}{n} \cdot \frac{1}{n} \cdot \frac{1}{n}$ unit cube, then $\frac{1}{n} \cdot \frac{1}{n} \cdot \frac{1}{n}$ unit cube, then determining how many of those unit cubes fill the base, and finally multiplying by the number of units in the height to find how many $\frac{1}{n} \cdot \frac{1}{n} \cdot \frac{1}{n} \cdot \frac{1}{n}$ unit cubes are in the prism. <u>6.G.2</u> 13) Apply volume formulas, V = bh and V = lwh, to find the volume of right rectangular prisms with fractional edge lengths in mathematical and real world contexts, making sense of the volume in terms of how many 1x1x1 unit cubes it represents and how many $\frac{1}{n} \cdot \frac{1}{n} \cdot \frac{1}{n} \cdot \frac{1}{n}$ unit cubes it represents. (Framework p.48)			Alignment for Outcomes 12-13: CA Framework p. 46 & 48 Flipbook p. 53-54 NC Unpacking p. 46-47 enVision, Topic 13: • Lesson 13-3 "Modeling Volume" • Lesson 13-4 "Volume with Fractional Lengths" • Lesson 13-5 "Use Objects and Reasoning"		
			6.G.2					

Unit #7: Statistics and Probability

(Approx. # of Days 20-30)

Content Standards: 6.SP.1-5

In this unit, students will be able to develop an understanding of statistical variability; how to look at, collect, and use data effectively; and how to represent aspects of the data.

Common Core State Standards-Mathematics:

Statistics and Probability 6.SP

Develop understanding of statistical variability.

- 1. Recognize a statistical question as one that anticipates variability in the data related to the question and accounts for it in the answers. For example, "How old am I?" is not a statistical question, but "How old are the students in my school?" is a statistical question because one anticipates variability in students' ages.
- 2. Understand that a set of data collected to answer a statistical question has a distribution which can be described by its center, spread, and overall shape.
- 3. Recognize that a measure of center for a numerical data set summarizes all of its values with a single number, while a measure of variation describes how its values vary with a single number.

Summarize and describe distributions.

- 4. Display numerical data in plots on a number line, including dot plots, histograms, and box plots.
- 5. Summarize numerical data sets in relation to their context, such as by: a. Reporting the number of observations.
 - b. Describing the nature of the attribute under investigation, including how it was measured and its units of measurement.
 - c. Giving quantitative measures of center (median and/or mean) and variability (interquartile range and/or mean absolute deviation), as well as describing any overall pattern and any striking deviations from the overall pattern with reference to the context in which the data were gathered.
 - d. Relating the choice of measures of center and variability to the shape of the data distribution and the context in which the data were gathered.

Standards for Mathematical Practice:

- SMP.1 Make sense of problems and persevere in solving them
- SMP.4 Model with mathematics
- SMP.5 Use appropriate tools strategically
- SMP.6 Attend to precision

ELD Standards to Support Unit:

Part I: Interacting in Meaningful Ways:

- S. Collaborative:
 - 8. Interacting with others in written English in various communicative forms16. Adapting language choices to various contexts
- T. Interpretive:
 - 17. Listening actively to spoken English in a range of social and academic contexts.
- U. Productive:

11. Supporting own opinions and evaluating others' opinions in speaking and writing.

Part II: Learning About How English Works

- Expanding and Enriching Ideas
 - 5. Modifying to add details.
- Connecting and Condensing Ideas
 - 6. Connecting Ideas
 - 7. Condensing Ideas

SEL Competencies:
Self-awareness
Self-management
Social awareness

Relationship skills

Responsible decision making

	Unit #7 Statistics and Probability						
Essential Questions	Assessments for Learning	Sequence of Learning Outcomes 6.SP.1, 6.SP.2, 6.SP.3, 6.SP.4, 6.SP.5	Strategies for Teaching and Learning	Differentiation (EL/SpEd/GATE)	Resources		
Essential Questions are thought- provoking, open-ended questions to be used within daily lessons that and are therefore connected to the Sequence of Learning Outcomes	address Diagnostic, Formative, and Summative assessments used	Sequence of Learning Outcomes is intentionally organized for student success. Each outcome is not necessarily intended to be taught within one class session. Each Outcome begins with Students will be able to	 Strategies to support Unit: From the CA Mathematics Framework <u>"Instructional Strategies"</u> chapter provides research-based strategies for teaching math, K-12 <u>"Supporting High Quality Common Core Instruction"</u> chapter addresses the development, implementation, and maintenance of high-quality, standards-based mathematics instructional programs <u>"Universal Design for Learning"</u> from CAST, the Center for Applied Special Technology 	formative assessment. See <u>Teaching Channel Video</u> Flexible grouping:	 CCSS Support for the Unit: CA Mathematics Framework Gr. 6 p. 50-55 Statistics and Probability Kansas Association of Teachers of Mathematics (KATM) 6th Grade Flipbook Provide illustrated examples, instructional strategies, additional resources/tools and misconceptions by standard. p. 59-73 Statistics and Probability North Carolina Department of Public Instructional strategies, additional resources/tools and misconceptions by standard. Provides illustrated examples, instructional strategies, additional resources/tools and misconceptions by standard. Provides illustrated examples, instructional strategies, additional resources/tools and misconceptions by standard. p. 50-57 Statistics and Probability Progressions for CCSS-M Narrative documents describing the progression of a topic across a number of grade levels, informed both by research on children's cognitive development and by the logical structure of mathematics. Progressions on Statistics and Probability Overview p. 2-3 Grade 6 p. 4-6 		

	Unit #7 Statistics and Probability						
	Essential Questions	Assessments for Learning	Sequence of Learning Outcomes 6.SP.1, 6.SP.2, 6.SP.3, 6.SP.4, 6.SP.5	Strategies for Teaching and Learning	Differentiation (EL/SpEd/GATE)	Resources	
•	What is a statistical question and how can you gather data?	For Outcome 1: <u>Examples of Statistical</u> <u>Questions</u> From Illustrative Mathematics: <u>Buttons</u>	 Recognize a statistical question as one that is measurable and has variability in response. 6.SP.1 		 Anchor Activities: Content-related Tasks for early finishers Game Investigation Partner Activity Stations 	CA Framework p.50-53 Progressions p. 4 Flipbook p. 59-60 NC Unpacking p. 50 enVision, Topic 14 • Lesson 14-1 "Statistical Questions"	
		 From HCPSS (Google Doc – 6.SP.1): <u>Statistical Questions</u> <u>Questions for Sorting</u> <u>Statistical and</u> <u>Non-Statistical</u> <u>Questions</u> <u>Categorical and</u> <u>Numerical Questions</u> <u>Categorical and</u> <u>Numerical Question</u> <u>Homework</u> 			Depth and Complexity Prompts/Icons: • Depth • Language of the Discipline • Patterns • Unanswered Questions • Rules • Trends • Big Ideas • Complexity Differentiation Resources from SCUSD Wikispace:		
					Use of math journals for differentiation and formative assessment. See		

	Unit #7 Statistics and Probability						
Essential Questions	Assessments for Learning	Sequence of Learning Outcomes 6.SP.1, 6.SP.2, 6.SP.3, 6.SP.4, 6.SP.5	Strategies for Teaching and Learning	Differentiation (EL/SpEd/GATE)	Resources		
 Why is the range between 1 and 6 calculated as 6-1 = 5, when there are actually 6 possible values, 1, 2, 3, 4, 5 and 6? What are the advantages of each type of graph used to represent data? What does the range tell you about the data? 	For Outcomes 2-3: From HCPSS (Google Doc) (For Outcome 2): <u>Shape of the Data</u> • <u>Teacher Resource</u> • <u>Closure Resource</u> • <u>Homework</u> From Google Docs: <u>Ear bud and pedestrian</u> <u>injuries task</u> • <u>Article for ear bud task</u>	 2) Design a statistical investigation and develop a plan for collecting data including how many data points will be collected, how they will be measured, the units of measurement and the process of collection. 6.SP.1 & 6.SP.2 3) Represent data on both a dot plot and a histogram. Determine the number of data points and their range. Make conjectures about the approximate center of the data. 6.SP.2, 6.SP.3, 6.SP.4 & 6.SP.5 	From Learn Zillion: Line plots, Histograms, and Box Plots:	Teaching Channel Video Flexible grouping: Content Interest Project/product Level (Heterogeneous/ Homogeneous) Tiered: 27) Independent Management Plan (Must Do/May Do) 28) Grouping a. Content b. Rigor w/in the concept c. Project-based learning d. Homework e. Grouping f. Formative Assessment			

Unit #7 Statistics and Probability						
Essential Questions	Assessments for Learning	Sequence of Learning Outcomes 6.SP.1, 6.SP.2, 6.SP.3, 6.SP.4, 6.SP.5	Strategies for Teaching and Learning	Differentiation (EL/SpEd/GATE)	Resources	
 What are the measures of central tendency? What is the usefulness of each measure of central tendency? What can cause differences between mean and median? 	For Outcomes 4-5 From Illustrative Mathematics: Puppy Weights Puzzle Times From Inside Mathematics: Baseball Players	 4) Understand measures of center by calculating mean and median of a given data set. Interpret mean and median numerically and on a dot plot and histogram. 6.SP.2, 6.SP.3, 6.SP.4 & 6.SP.5 5) Compare mean and median for a given data set, informally making sense of why they are similar and/or different based on the shape and spread of the data. 6.SP.2, 6.SP.3, 6.SP.4 & 6.SP.5 	Measures of Center in 6 th grade are: Median, Mean From Learn Zillion: <u>Finding Mean:</u> <u>Finding Median:</u>	 Stations Depth and Complexity Prompts/Icons: Depth Language of the Discipline Patterns Unanswered Questions Rules Trends Big Ideas Complexity Differentiation Resources from <u>SCUSD Wikispace</u>: 	For Outcomes 4 & 5: CA Framework p.50-55 Progressions p. 4-6 Flipbook p. 59-73 NC Unpacking p. 50-57 enVision, Topic 14 • Lesson 14-3 "Mean" • Lesson 14-4 "Median, Mode, Range"	

Unit #7 Statistics and Probability							
Essential Questions	Assessments for Learning	Sequence of Learning Outcomes 6.SP.1, 6.SP.2, 6.SP.3, 6.SP.4, 6.SP.5	Strategies for Teaching and Learning	Differentiation (EL/SpEd/GATE)	Resources		
 What are the advantages of each type of graph used to represent data? What is variability and what are the different ways it is measured? What does the range tell you about the data? What do you need to represent a box plot? What is not represented by a box plot? 	For Outcomes 6-9: From Illustrative Mathematics: Electoral College From HCPSS (Google Doc): Cyberbullying Doesn't Add Up • Analyzing Graphs Student Question Resource • Analyzing Graphs Homework	 6) Investigate the variability of data by calculating and interpreting the MAD (Mean Absolute Deviation) of a set of data that can be represented with a dot plot or histogram. 6.SP.2, 6.SP.3, 6.SP.4 & 6.SP.5 7) Find the median, upper and lower quartile, minimum and maximum and use them to create a box plot to represent a given data set. 6.SP.2, 6.SP.3, 6.SP.4 & 6.SP.5 8) Investigate the variability of data represented by a box plot by calculating and interpreting the interquartile range. 6.SP.2, 6.SP.3, 6.SP.4 & 6.SP.5 9) Compare and contrast the different ways of representing a given set of data from a graph, measures of center, and measures of variability, recognizing which graphs and measures are more appropriate given the center and shape. 6.SP.2, 6.SP.3, 6.SP.4 & 6.SP.5 	From Learn Zillion: Line plots, Histograms, and Box Plots: From Learn Zillion: Range, Interquartile Range, and MAD Finding Interquartile Range (IQR):		 For Outcomes 6-7: CA Framework p.50-55 Progressions p. 4-6 Flipbook p. 59-73 NC Unpacking p. 50-57 enVision, Topic 14 Lesson 14-7 "Measures of Variability" Lesson 14-6 "Box Plots" CA Framework p.50-55 Progressions p. 4-6 Flipbook p. 59-73 NC Unpacking p. 50-57 enVision, Topic 14 Lesson 14-8 "Appropriate Use of Statistical Measures" CA Framework p.50-55 Progressions p. 4-6 Flipbook p. 59-73 NC Unpacking p. 50-57 enVision, Topic 14 Lesson 14-8 "Appropriate Use of Statistical Measures" CA Framework p.50-55 Progressions p. 4-6 Flipbook p. 59-73 NC Unpacking p. 50-57 enVision, Topic 14 Lesson 14-9 "Summarizing Data Distributions" Lesson 14-10 "Try, Check, and Revise" 		